

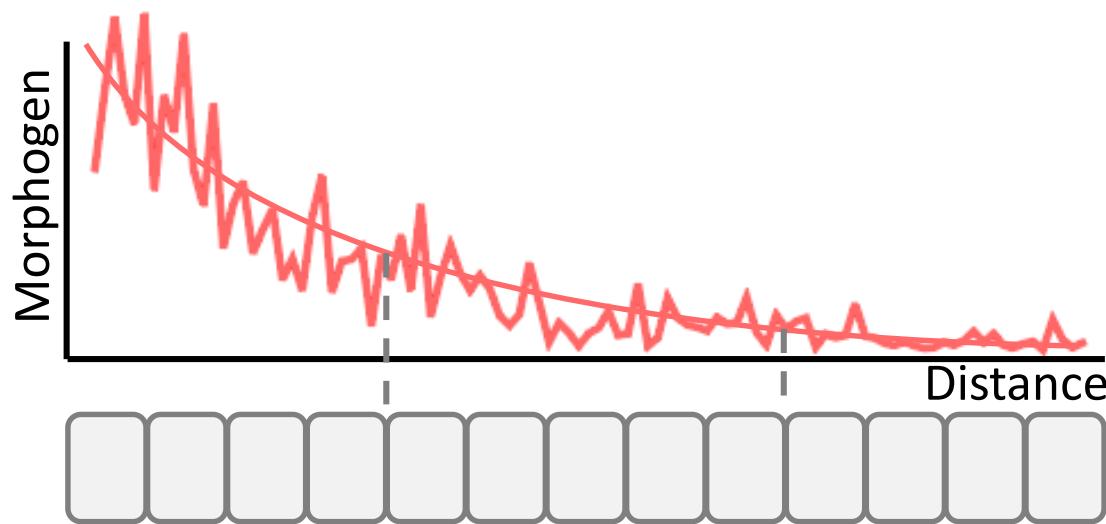
How is information decoded in developmental systems?

Marcin Zagórski

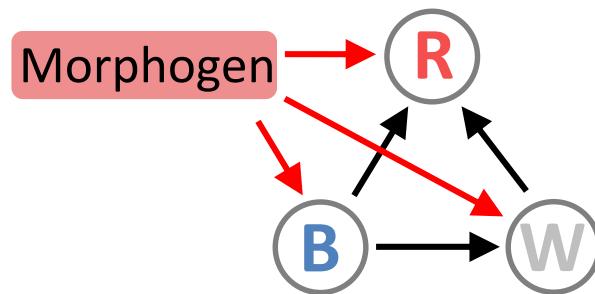
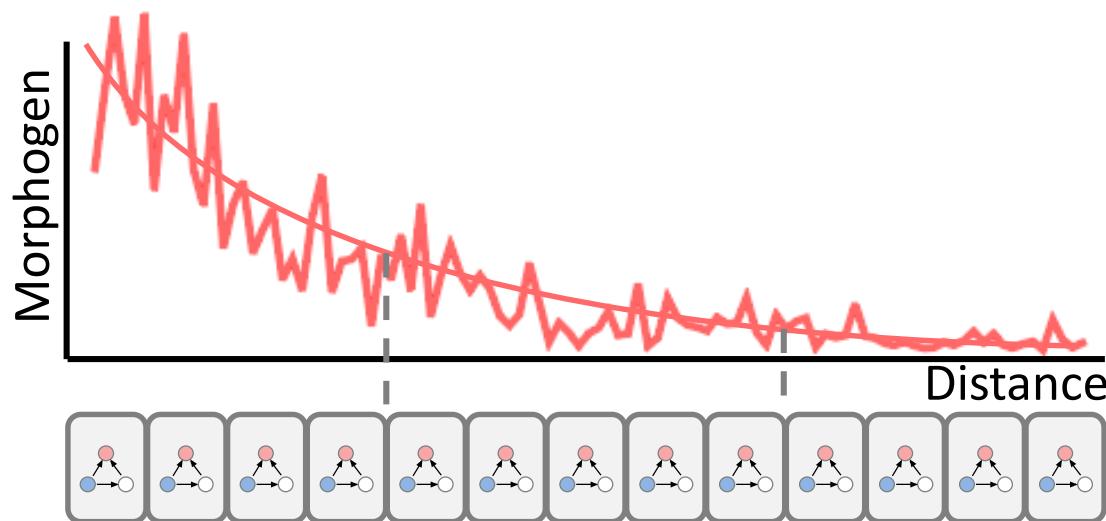


JAGIELLONIAN UNIVERSITY
IN KRAKÓW

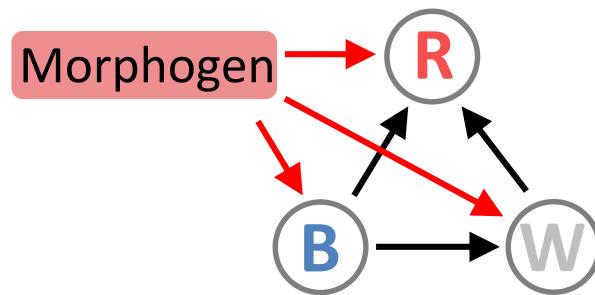
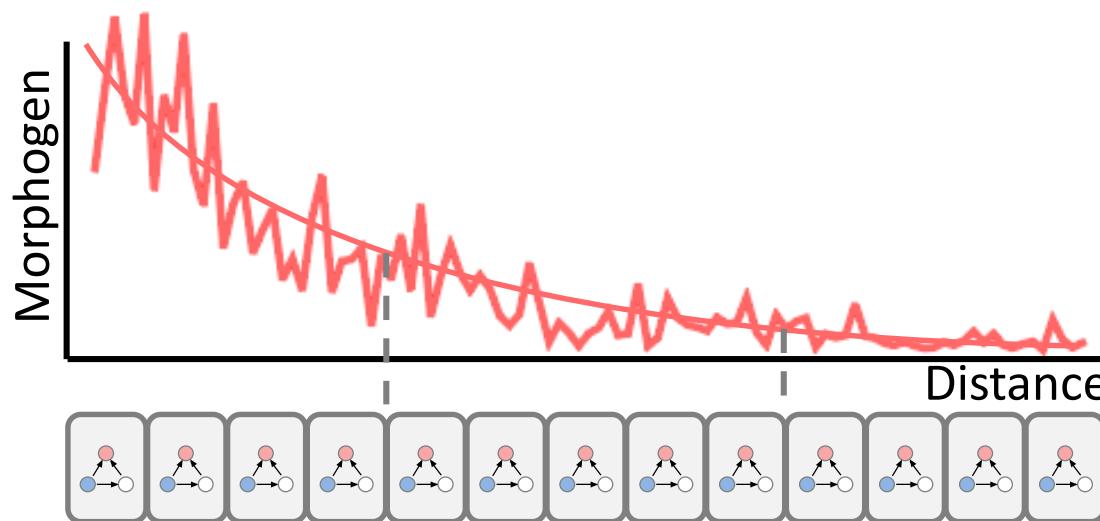
Morphogen gradients provide positional information establishing coordinate system for the developing tissue



Morphogen gradients provide positional information establishing coordinate system for the developing tissue



Morphogen gradients provide positional information establishing coordinate system for the developing tissue



Gene expression pattern



The gene regulatory network acts as an information decoder that specifies target pattern

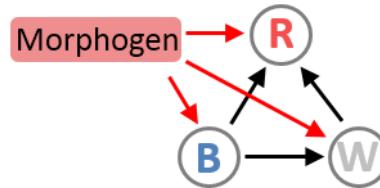
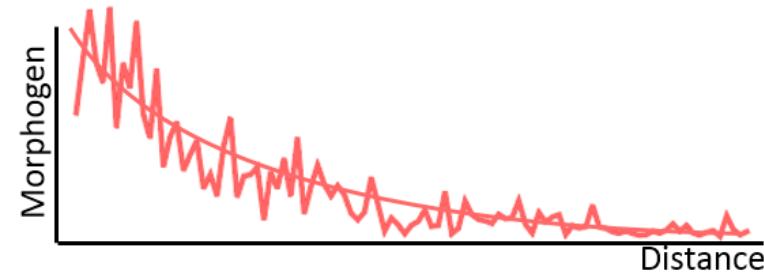
Input signal



Information
decoder



Output signal



Gene expression pattern



Optimal processing of information allows for pattern prediction without gene regulatory network

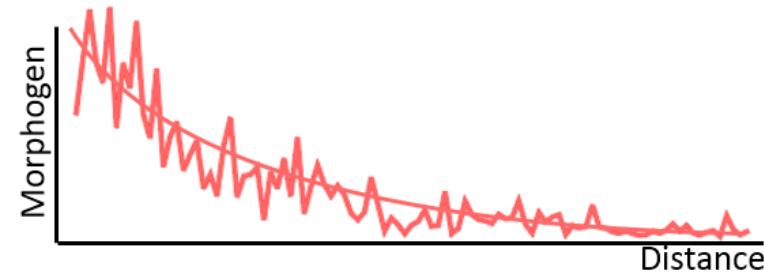
Input signal



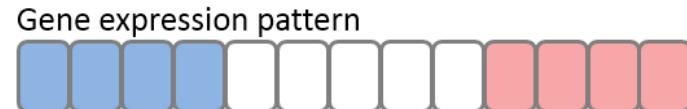
Information
decoder



Output signal



Optimal processing of
positional information



Optimal decoder contains all the information that any cellular or computational mechanism could extract from input signals

Measured signal $\{g_i(x)\} = \{g_1(x), g_2(x), g_3(x), g_4(x)\}, \quad K = 4$

Signal distribution at every x

$$P(\{g_i\}|x) = \frac{1}{\sqrt{(2\pi)^K \det[\hat{\mathcal{C}}(x)]}} \exp \left\{ -\frac{1}{2} \sum_{i,j=1}^K (g_i - \bar{g}_i(x)) (\hat{\mathcal{C}}^{-1}(x))_{ij} (g_j - \bar{g}_j(x)) \right\}$$

Optimal decoder from
Bayes' rule

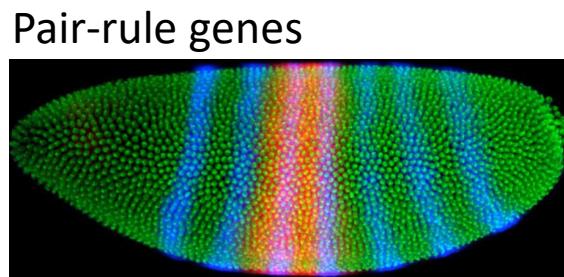
$$P(x^*|\{g_i\}) = \frac{1}{Z(\{g_i\})} P(\{g_i\}|x^*) P_X(x^*)$$

Decoding map

$$P_{map}^\alpha(x^*|x) = P(x^*|\{g_i\}) \Big|_{\{g_i\}=\{g_i^\alpha(x)\}}$$

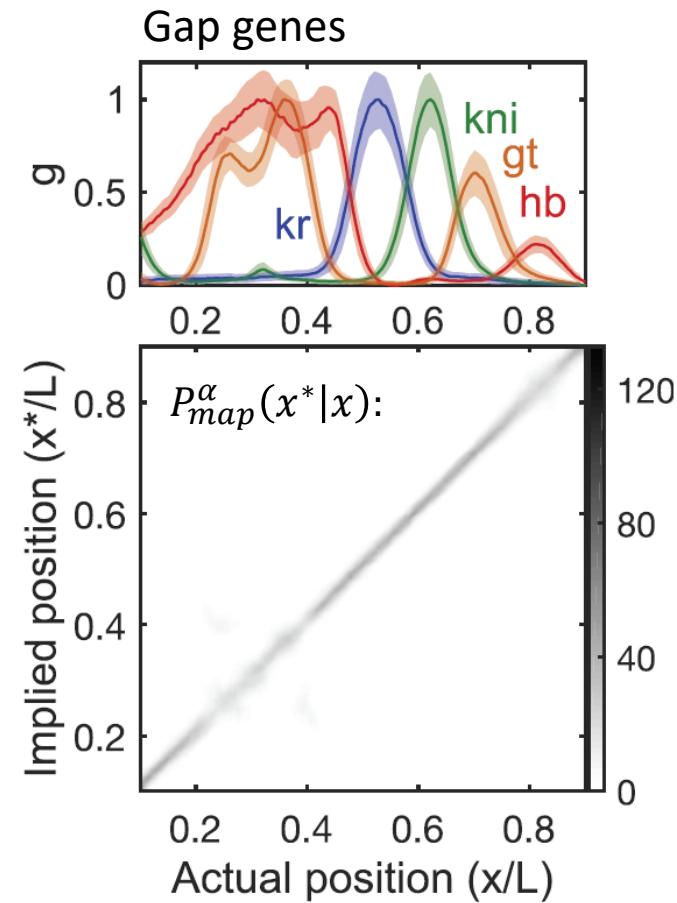
Tkacik et al., Genetics, 2015
Zagorski et al., Science, 2017
Petkova et al., Cell, 2019

In fruit fly decoding of input signals results in pattern specification with 1% positional error

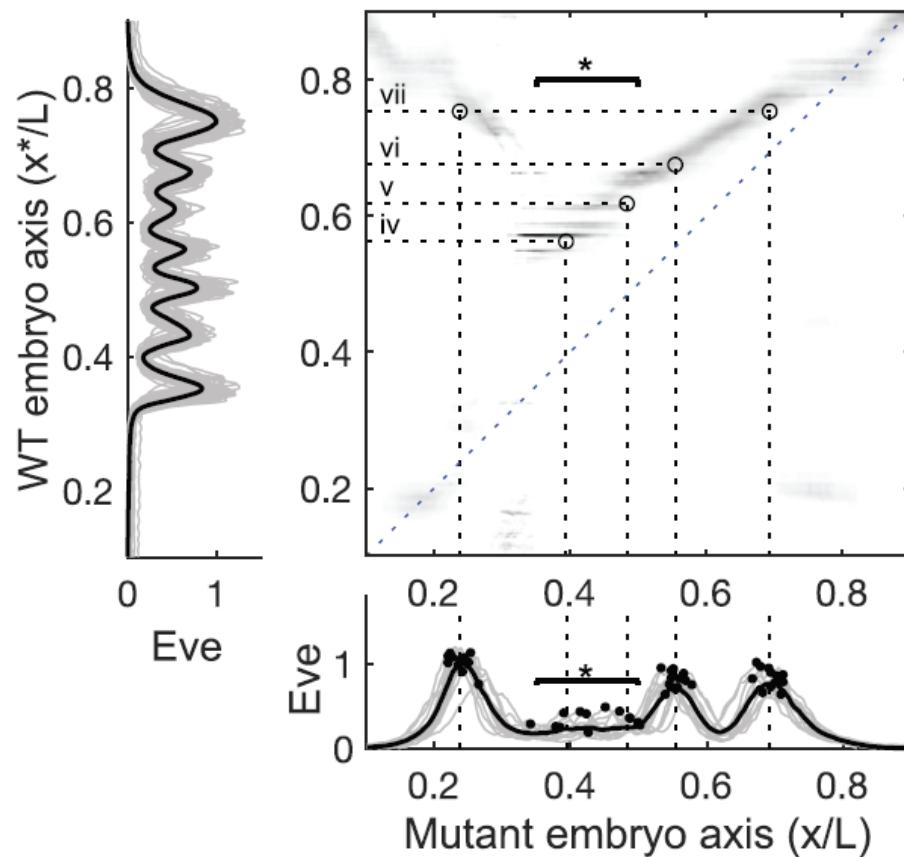


ittakes30.files.wordpress.com/2010/06/drosophila-eve.jpg

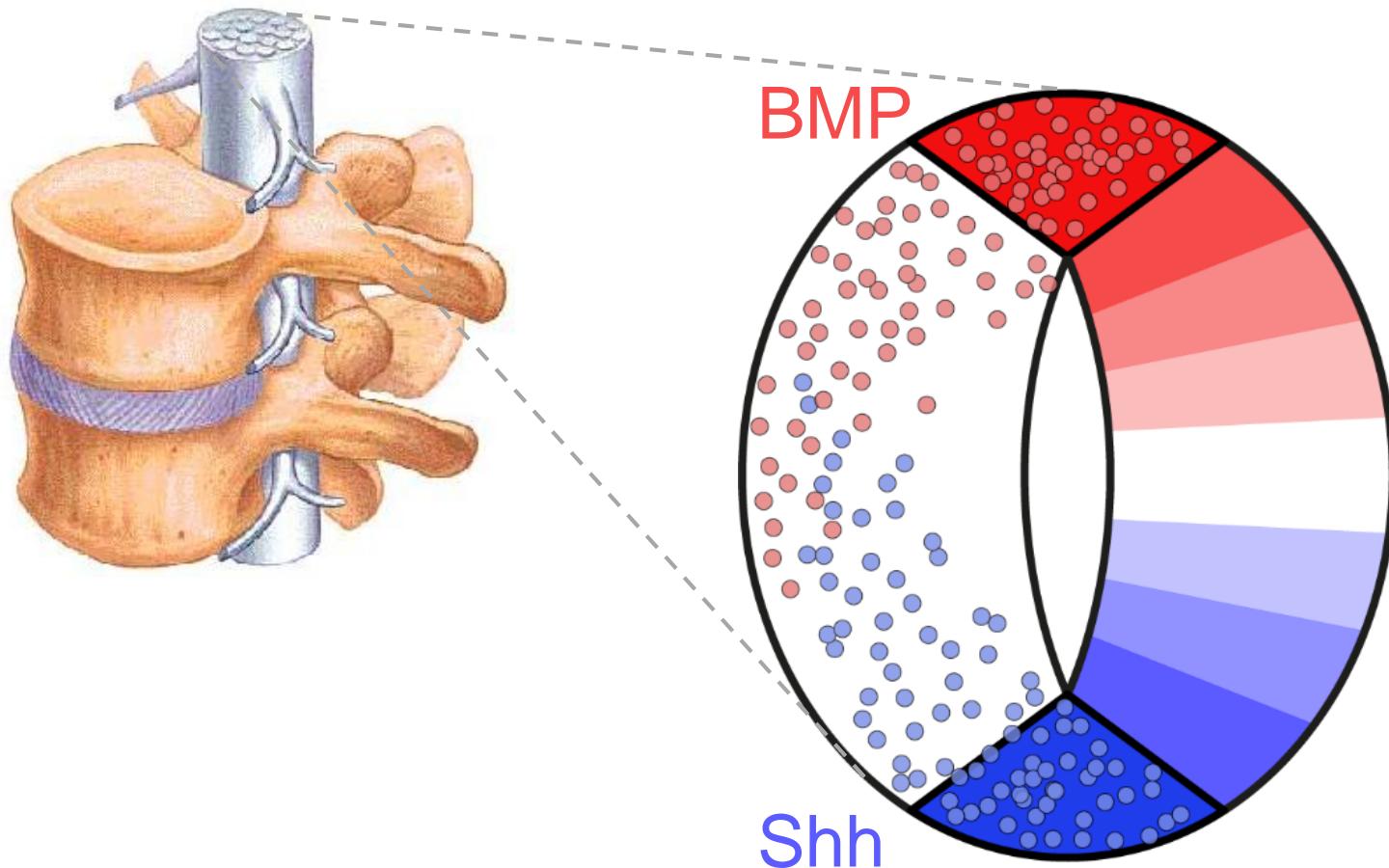
$\{g_i(x)\}$:



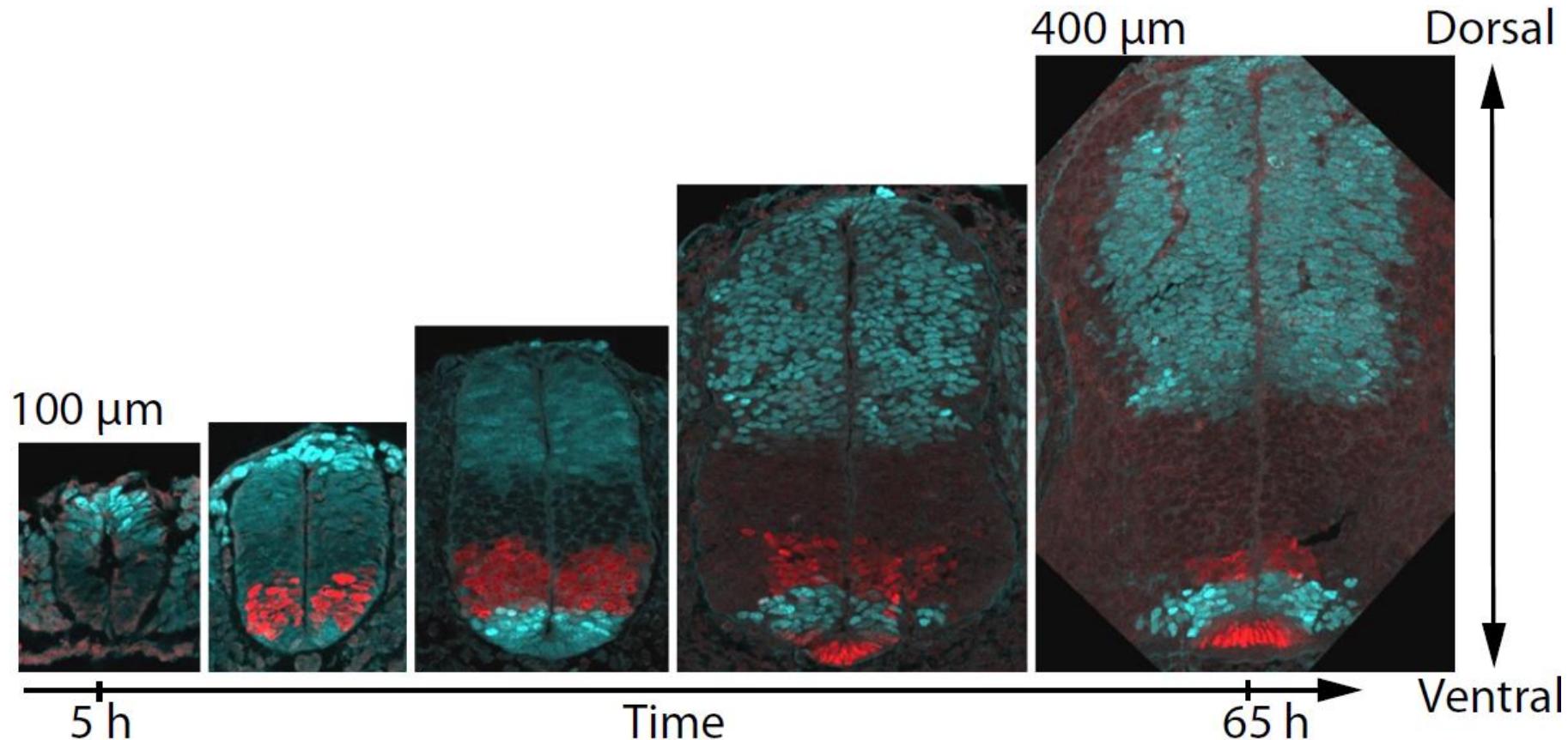
The decoding map correctly predicts shifts, disappearance and duplications in 70 pair-rule stripes in mutant embryos



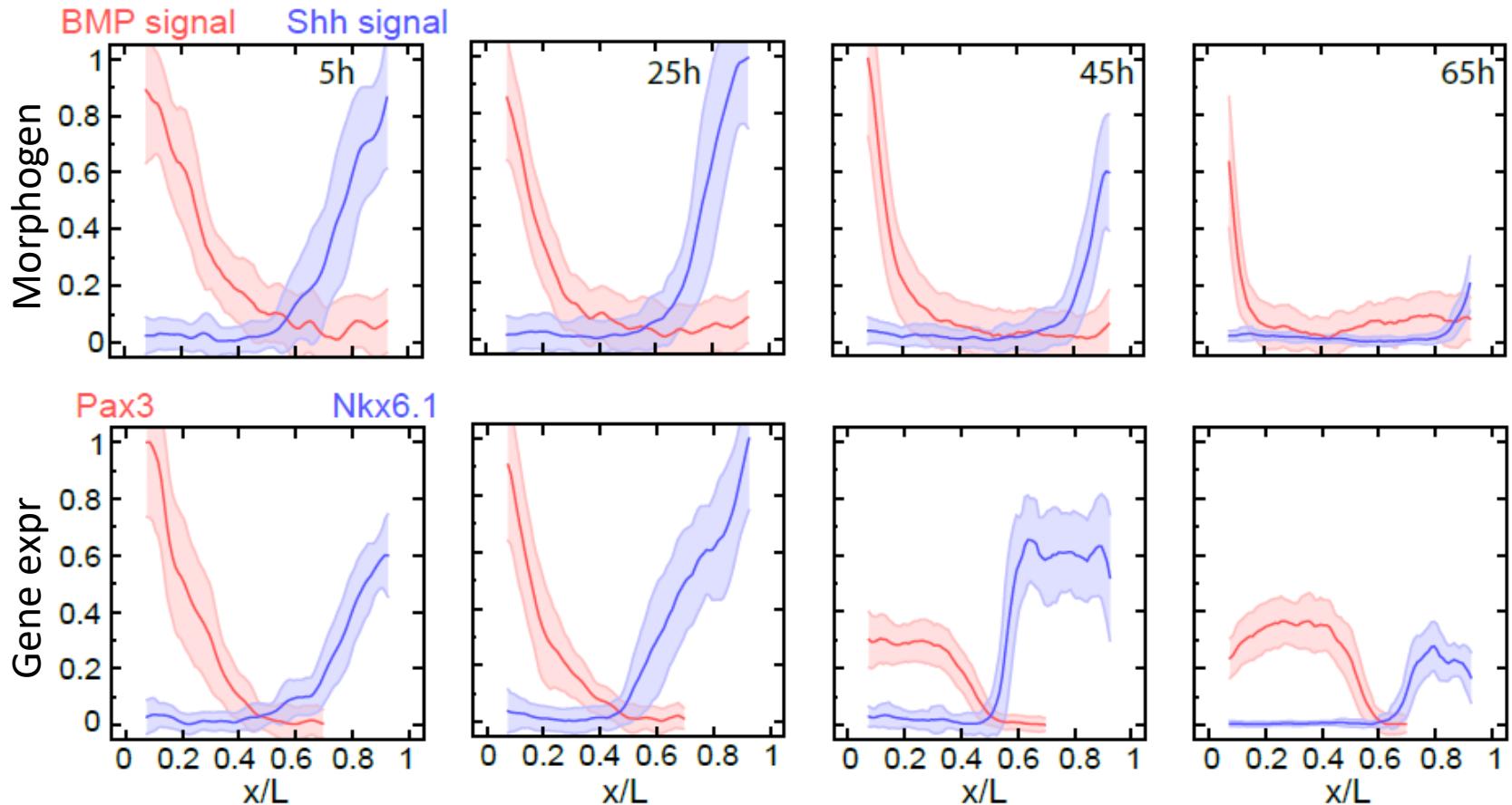
Morphogen signaling gradients establish a striped pattern of neural progenitors



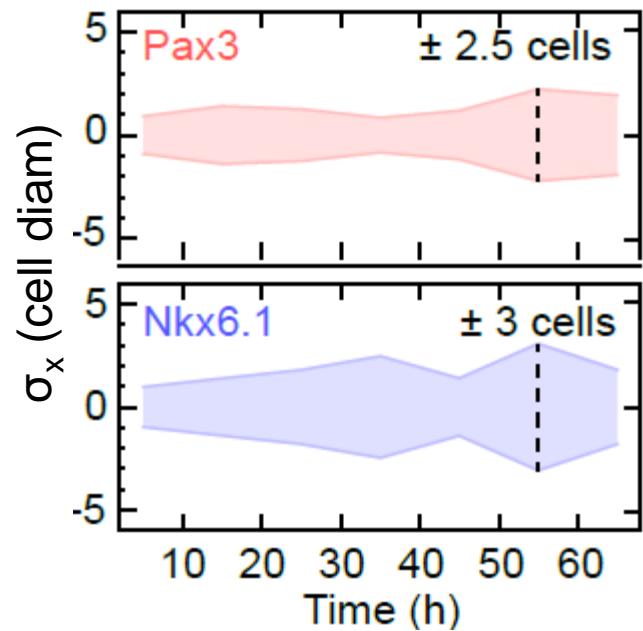
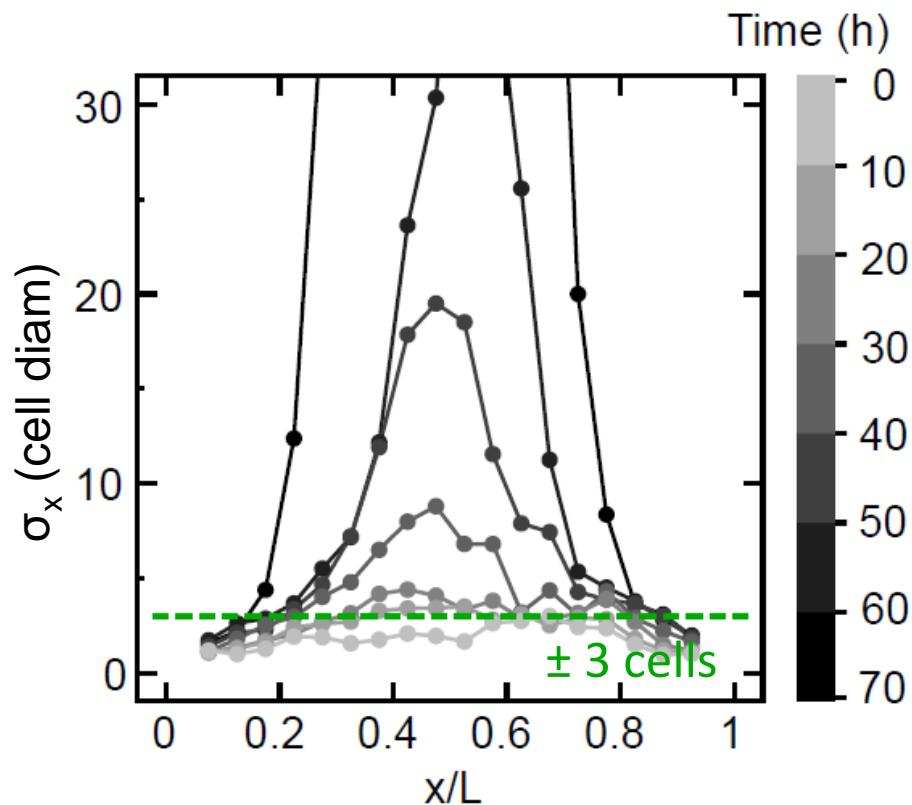
The striped pattern of gene expression domains is established progressively



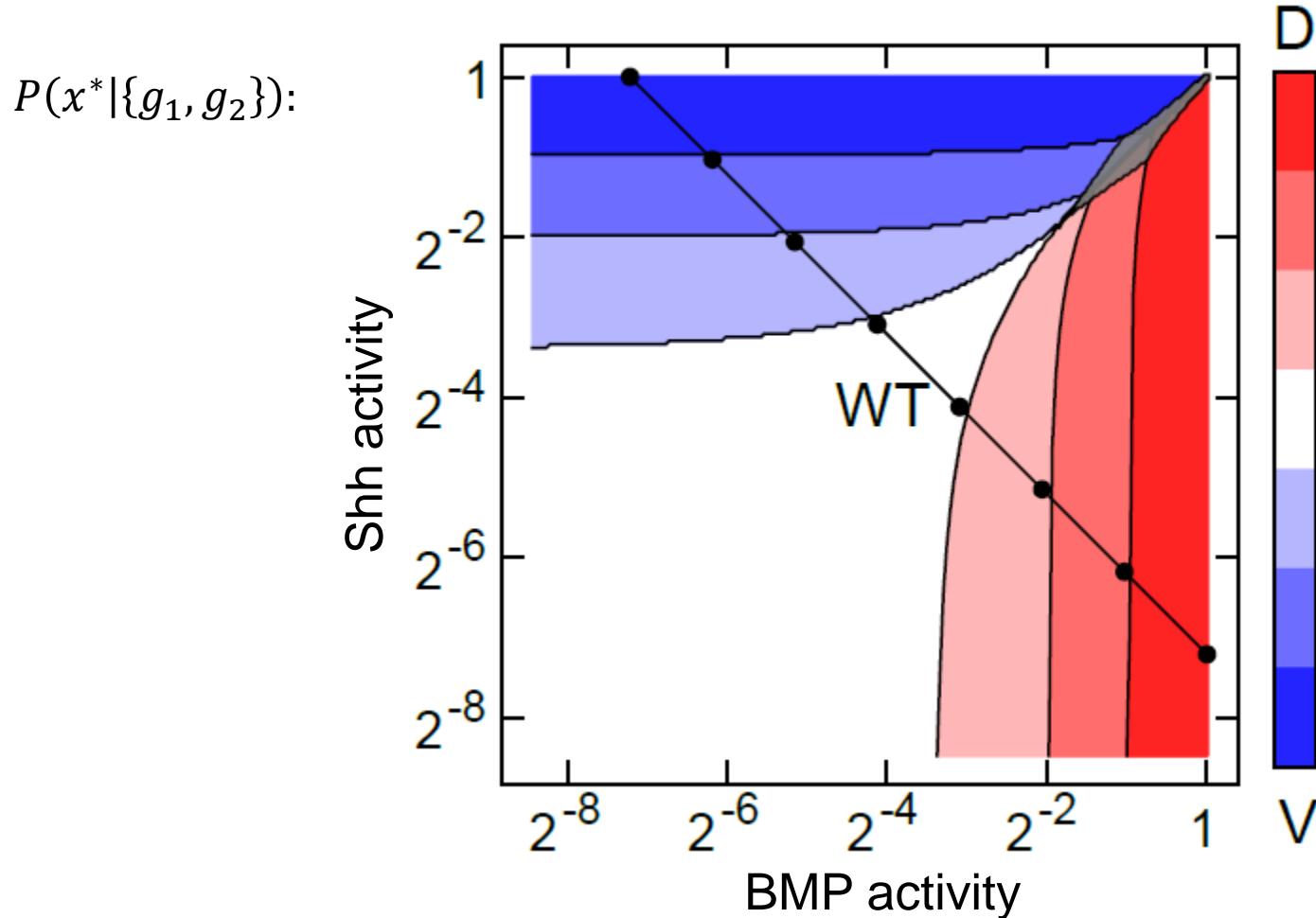
The morphogen signaling profiles do not scale with the embryo size



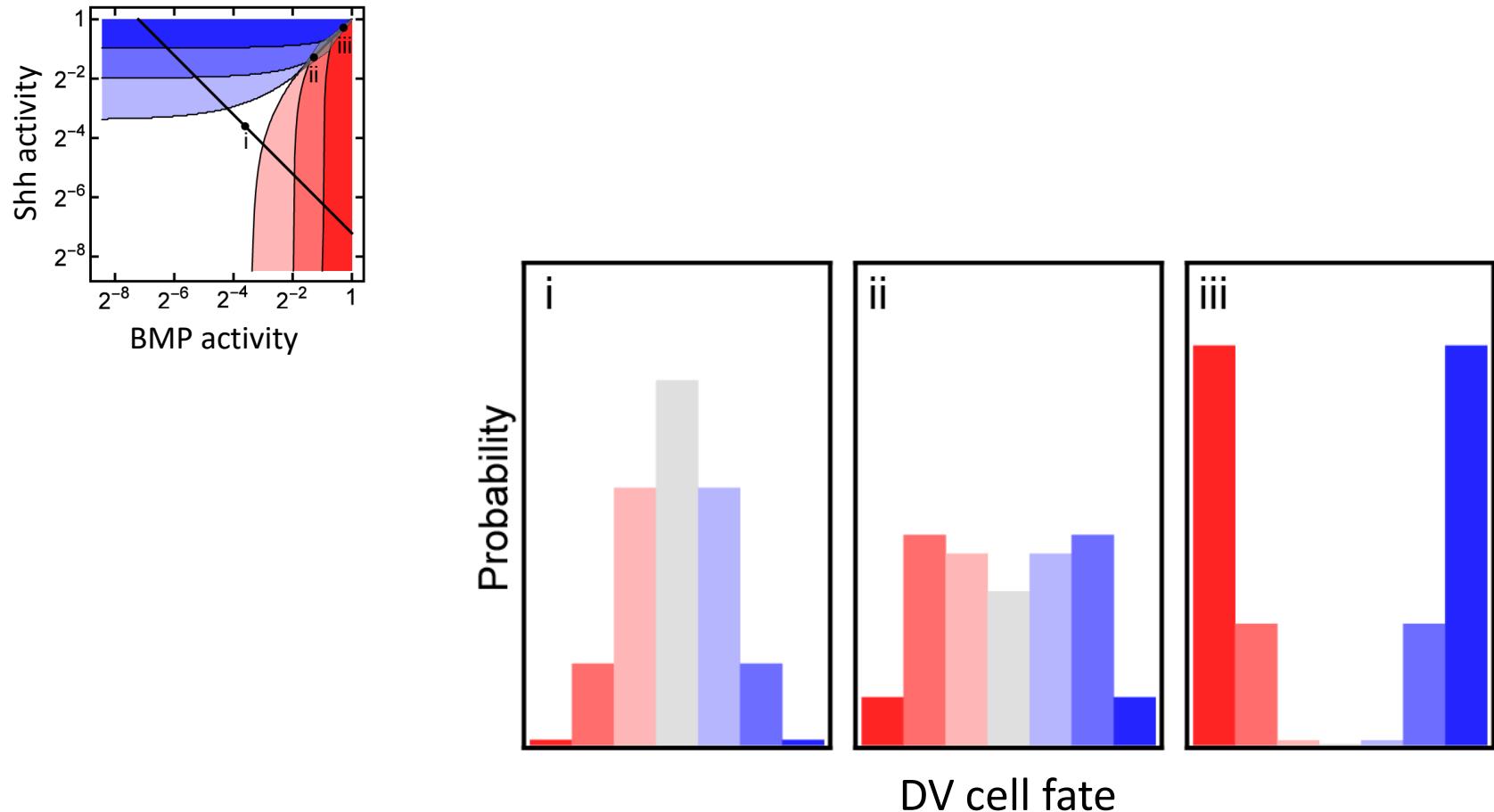
The initial morphogen positional error corresponds to the boundary imprecision at later stages



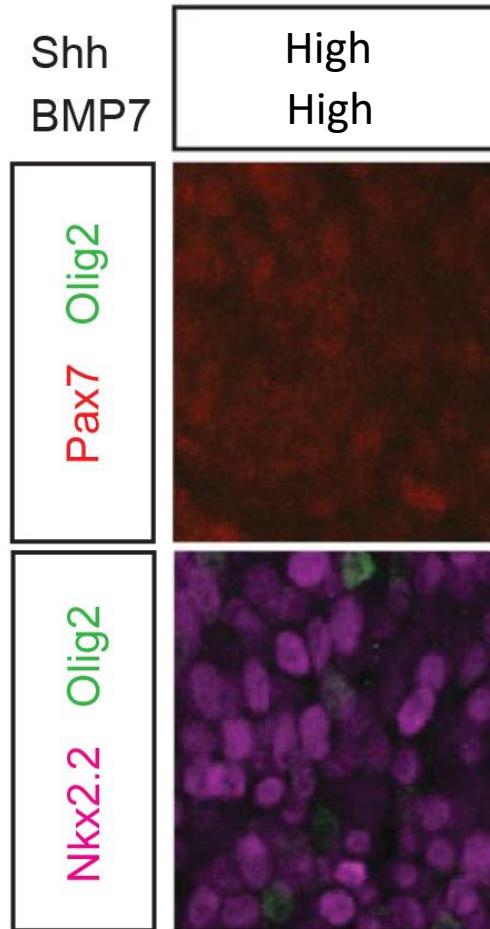
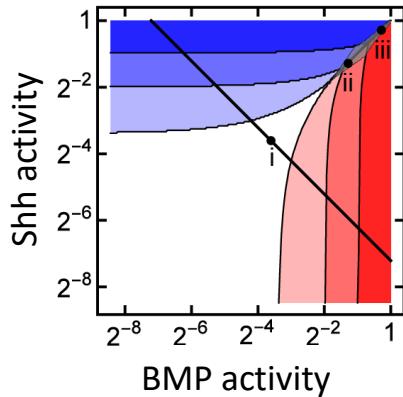
Cells interpret the opposing morphogen signals using an optimal decoding strategy



Decoding map predicts bimodal *posterior* distribution of cell fates for high morphogen concentrations



The predicted bimodal distribution of cell fates is consistent with explant experiments



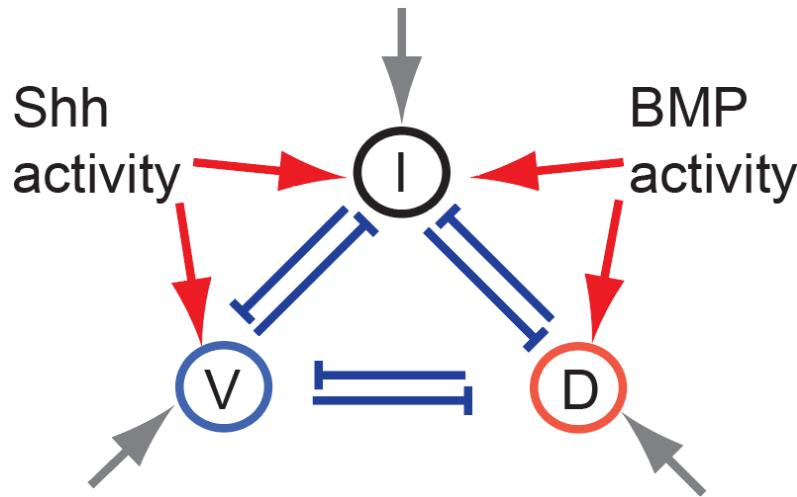
Red cells: Dorsal fates

Green cells: Intermediate fates

Violet cells: Ventral fates

Green cells: Intermediate fates

The morphogens activate gene regulatory network (GRN) to specify cell fate



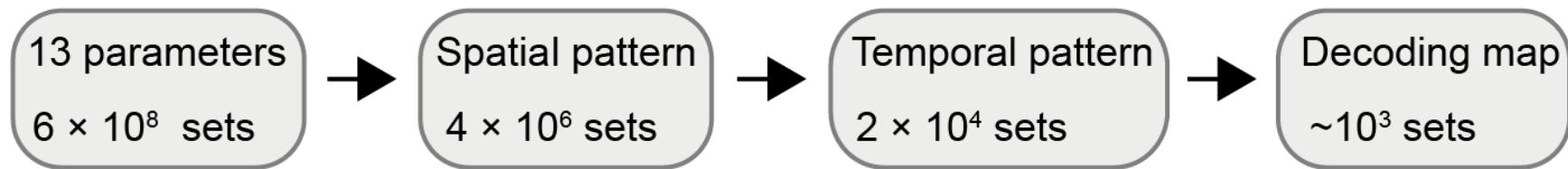
$$\frac{d[D]}{dt} = \alpha_D \frac{\kappa_D + c_{B \rightarrow D} \kappa_D [BMP]}{(1 + K_{V \rightarrow D}[V])^{m_{V \rightarrow D}} (1 + K_{I \rightarrow D}[I])^{m_{I \rightarrow D}} + \kappa_D + c_{B \rightarrow D} \kappa_D [BMP]} - \gamma_D [D]$$

$$\frac{d[V]}{dt} = \alpha_V \frac{\kappa_V + c_{S \rightarrow V} \kappa_V [Shh]}{(1 + K_{D \rightarrow V}[D])^{m_{D \rightarrow V}} (1 + K_{I \rightarrow V}[I])^{m_{I \rightarrow V}} + \kappa_V + c_{S \rightarrow V} \kappa_V [Shh]} - \gamma_V [V]$$

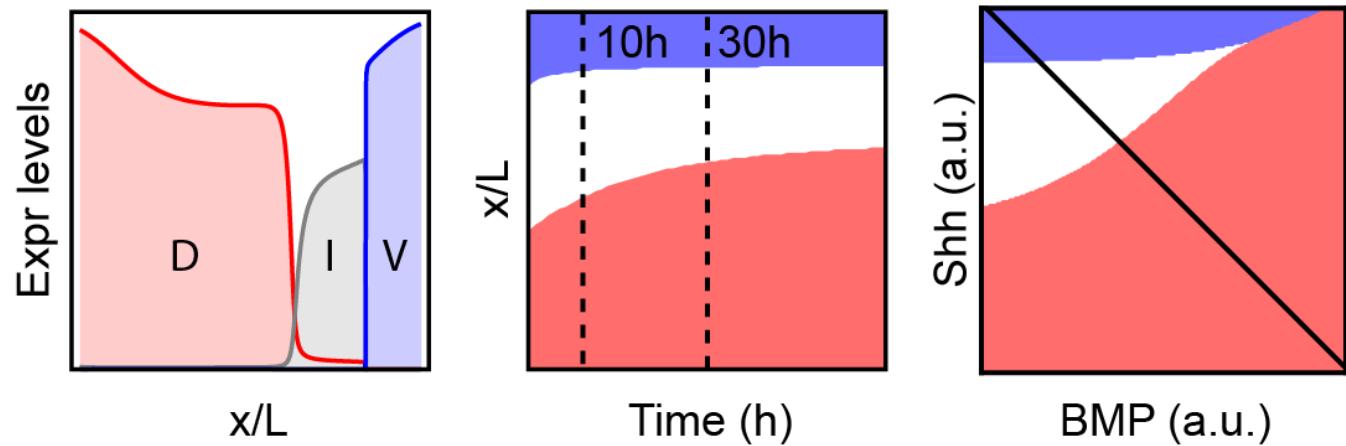
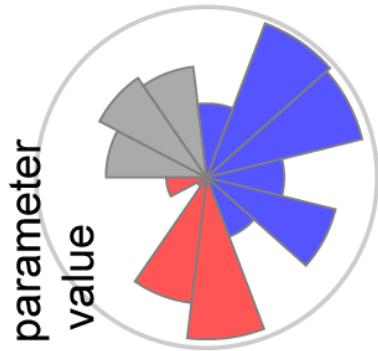
$$\frac{d[I]}{dt} = \alpha_I \frac{\kappa_I + c_{S \rightarrow I} \kappa_I [Shh] + c_{B \rightarrow I} \kappa_I [BMP]}{(1 + K_{D \rightarrow I}[D])^{m_{D \rightarrow I}} (1 + K_{V \rightarrow I}[I])^{m_{V \rightarrow I}} + \kappa_I + c_{S \rightarrow I} \kappa_I [Shh] + c_{B \rightarrow I} \kappa_I [BMP]} - \gamma_I [I]$$

Computational screen resulted in a set of successful GRNs consistent with experimental observations

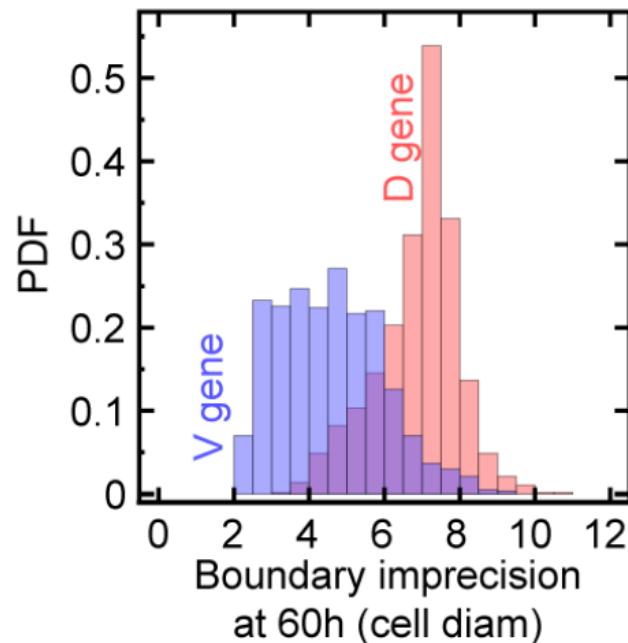
screen:



example:

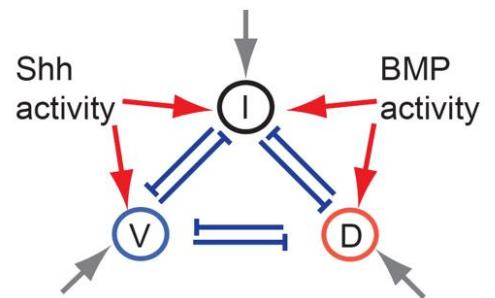
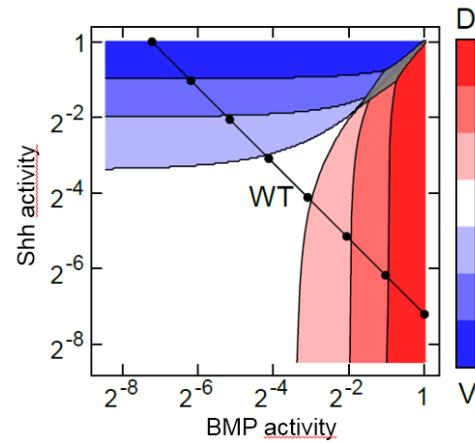
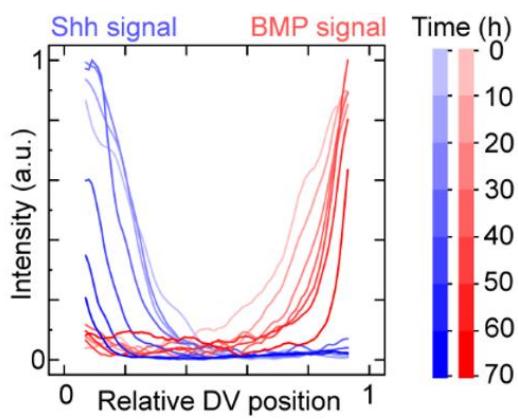


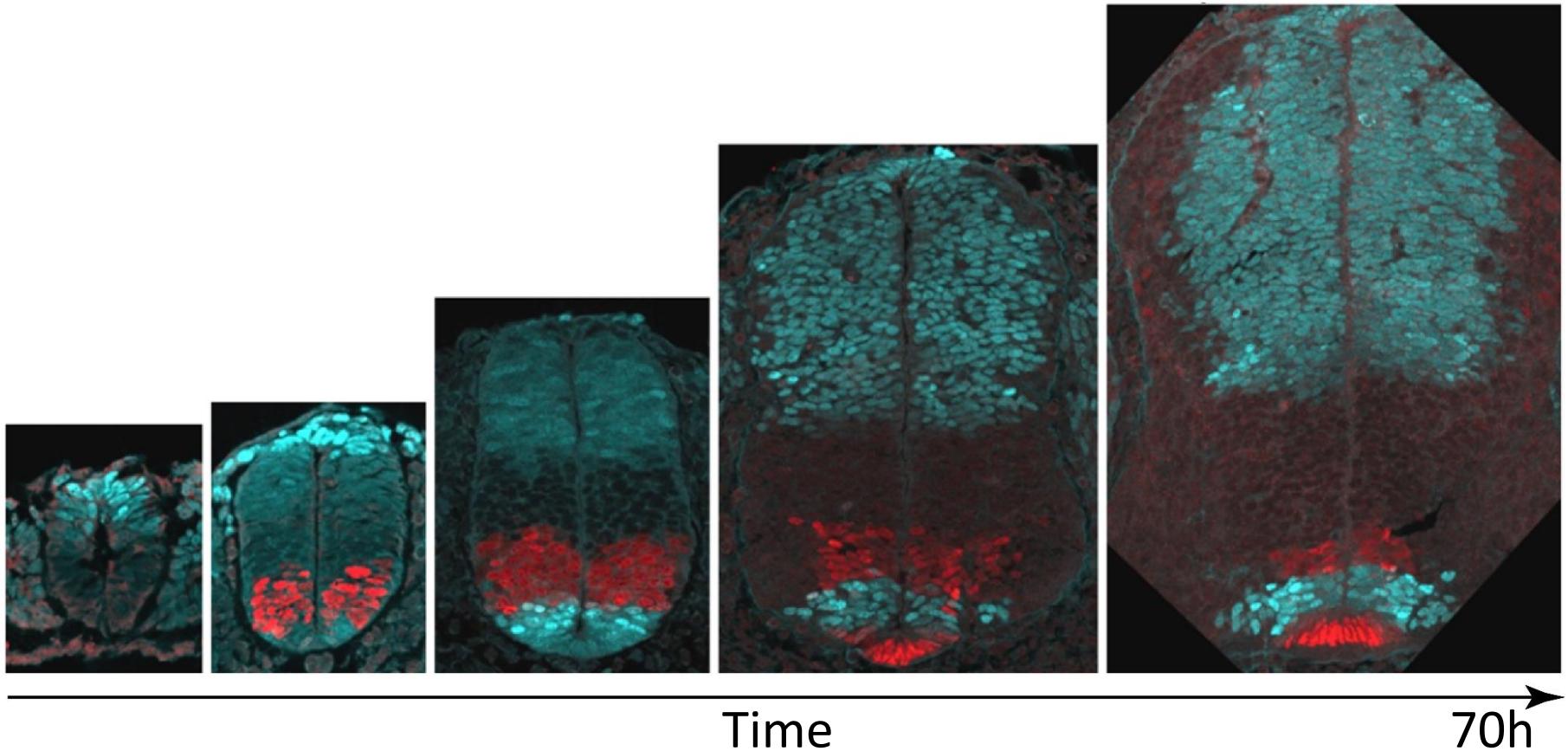
The target gene pattern established by GRNs resulted in a wide range of boundary imprecision



Summary

- ▶ Positional information is decoded with precision close to theoretical limit of decoding of noisy signals
- ▶ Regulatory mechanisms acting at the single cell level decode positional information
- ▶ Is the optimal decoding a fundamental principle characterizing pattern specification in developmental systems?





Acknowledgements: Anna Kicheva (IST Austria), Gašper Tkačik (IST Austria), Tobias Bollenbach (Univ Cologne), James Briscoe (Francis Crick Institute, UK)



National
Science
Centre
Poland

*The project is financed by the
National Science Centre, Poland*

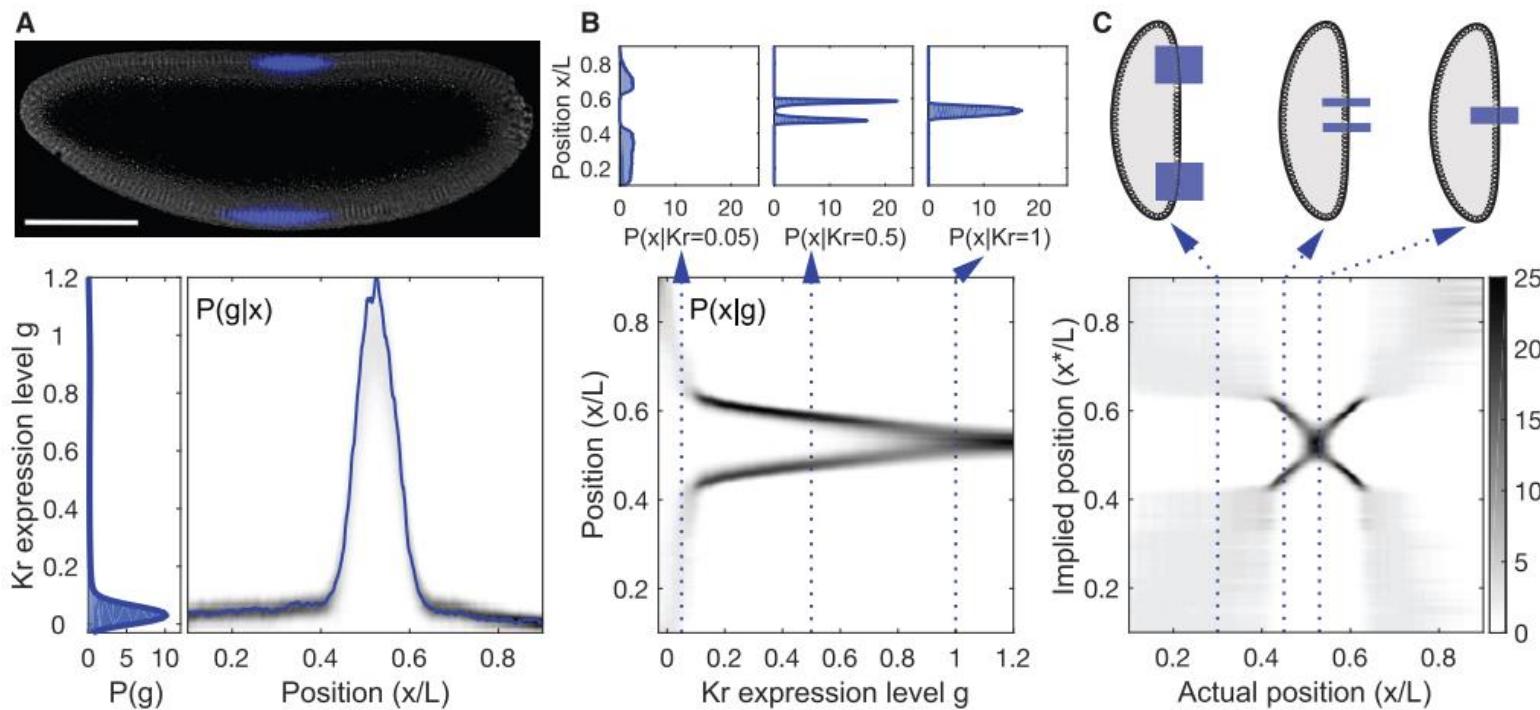


*The project is financed by the Polish
National Agency for Academic Exchange*

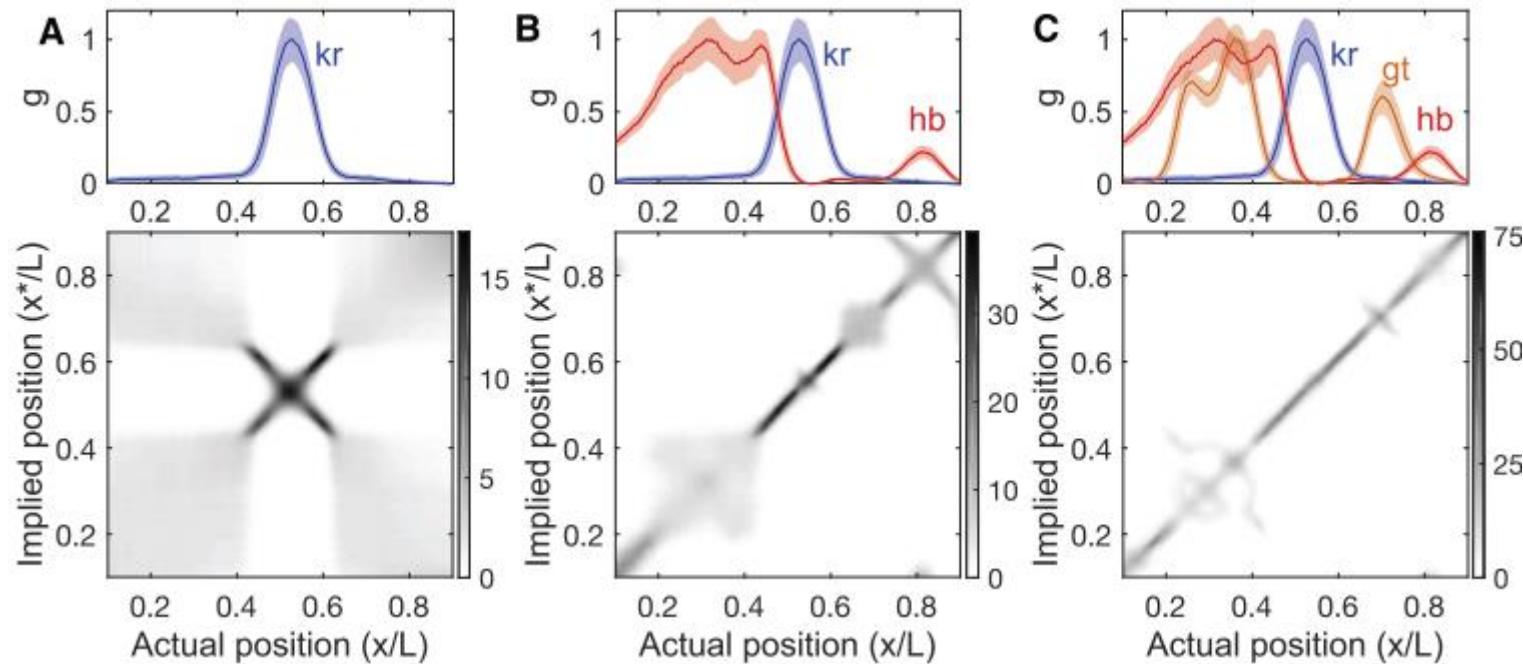
Future directions

- ▶ To what extent the formation of the morphogen source regions affects morphogen profiles?
- ▶ What type of regulatory mechanisms affecting morphogen spreading are optimal for minimizing positional error?
- ▶ How does temporal progression of information decoding affect pattern decoding?
- ▶ Can self-organizing modes of pattern specification increase information capacity of morphogen decoding?

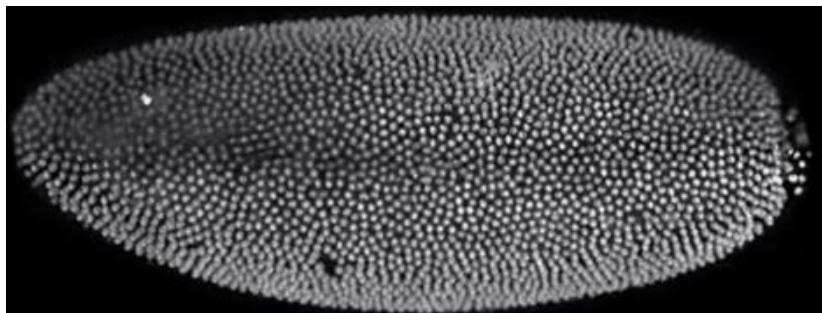
Coding and decoding positions in fly embryos



Coding and decoding positions in fly embryos



Cells acquire specific fates during organisms development

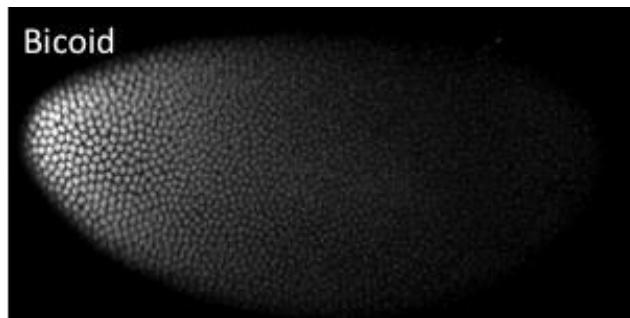


i.imgur.com/NKIMPmp.gif

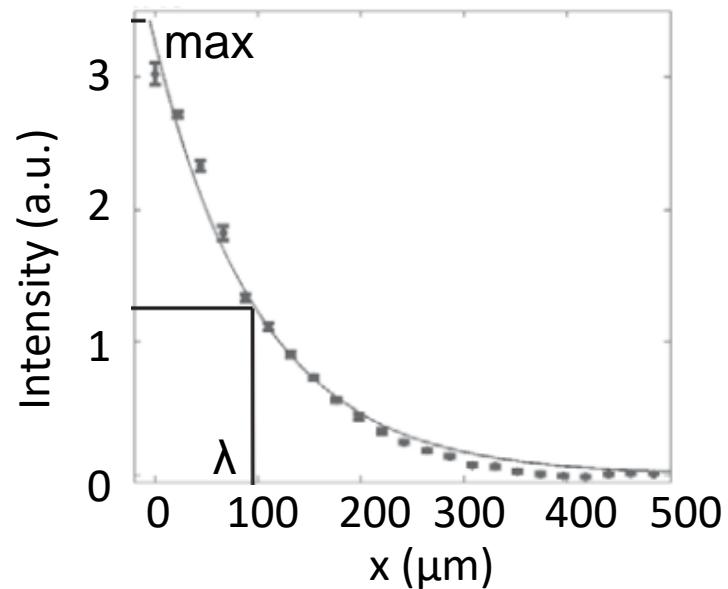
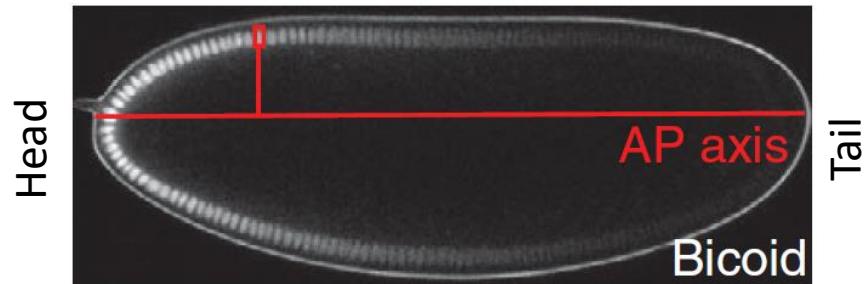


www.sciencebuzz.com

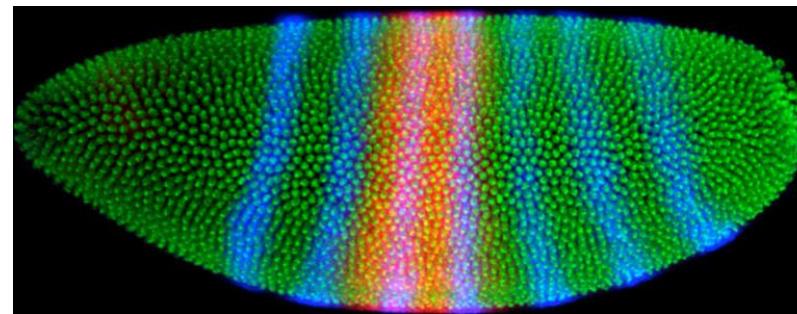
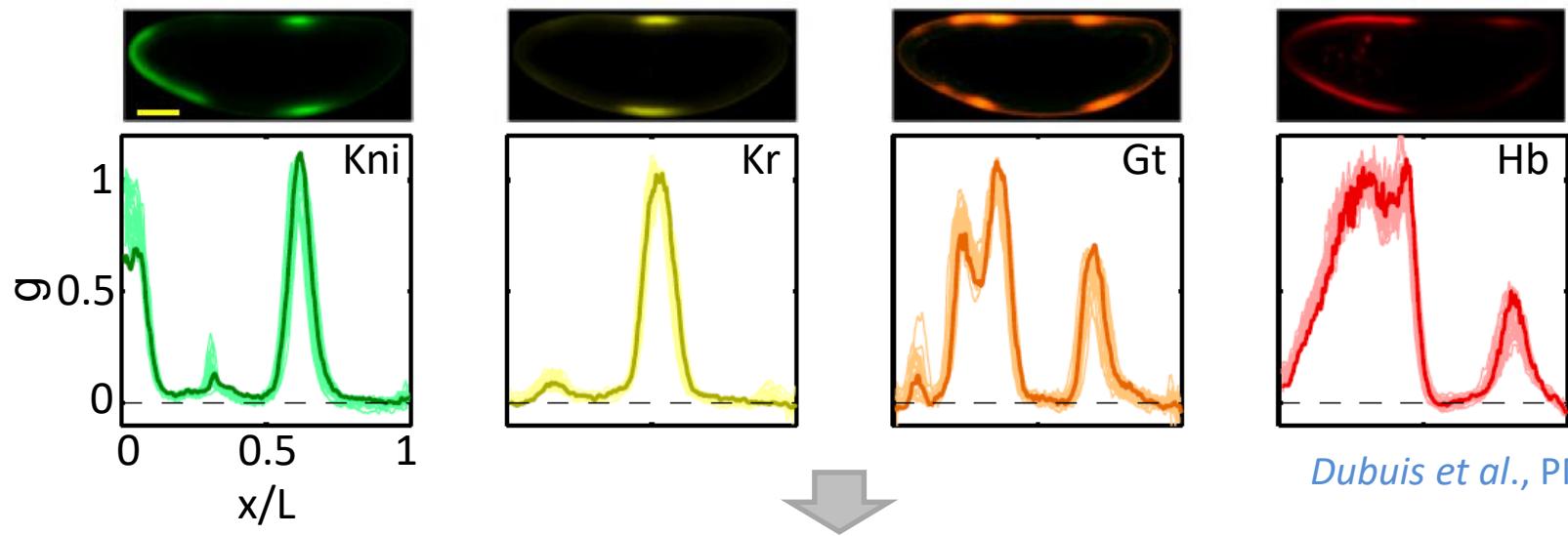
Bicoid proteins form a concentration gradient providing coordinate system for developing embryo



as.nyu.edu/faculty/stephen-small.html

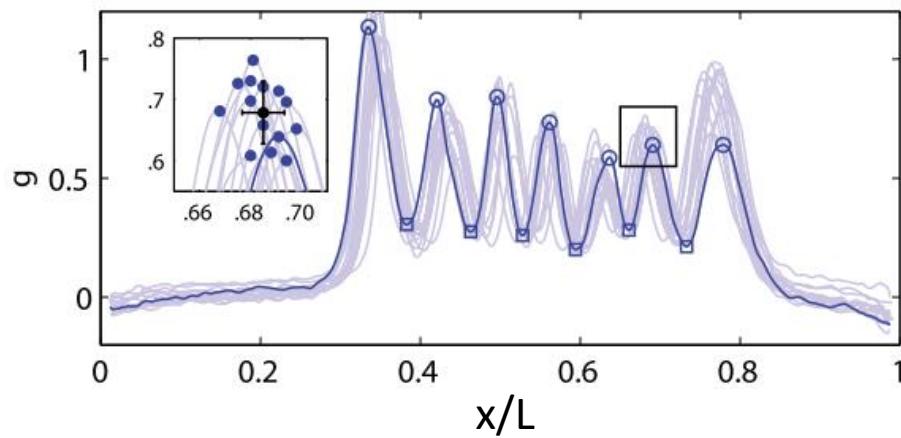
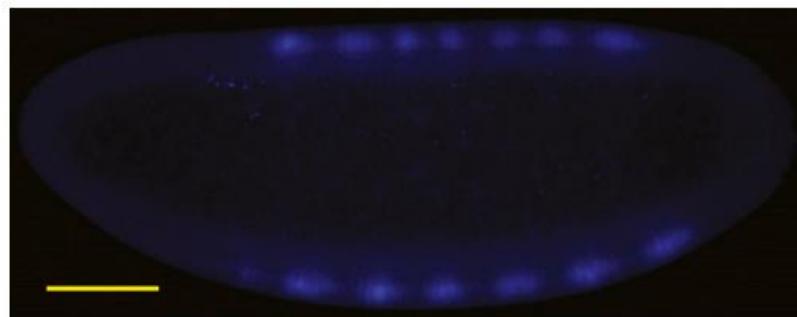


In fruit fly expression levels of 4 gap genes specify striped pattern of pair-rule genes



ittakes30.files.wordpress.com/2010/06/drosophila-eve.jpg

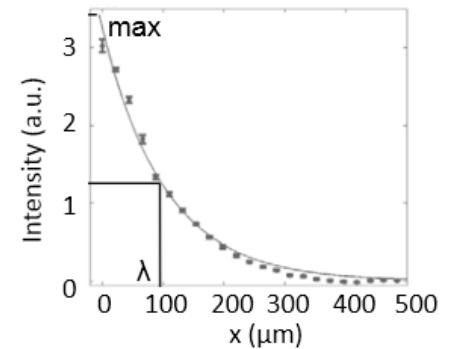
The information is decoded to specify gene expression pattern; output



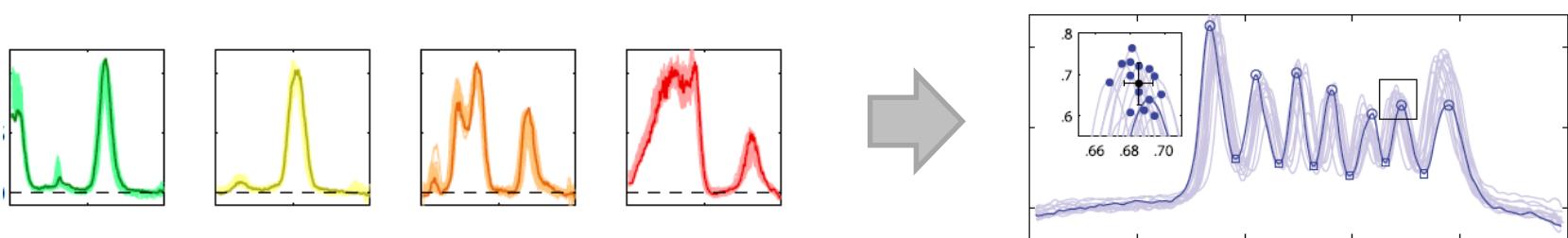
- ▶ Input: $I = 4.1 \pm 0.2$ bits, Output: $I = 4.3$ bits.

Interim summary

- ▶ Morphogens provide a coordinate system for patterning of developing tissues

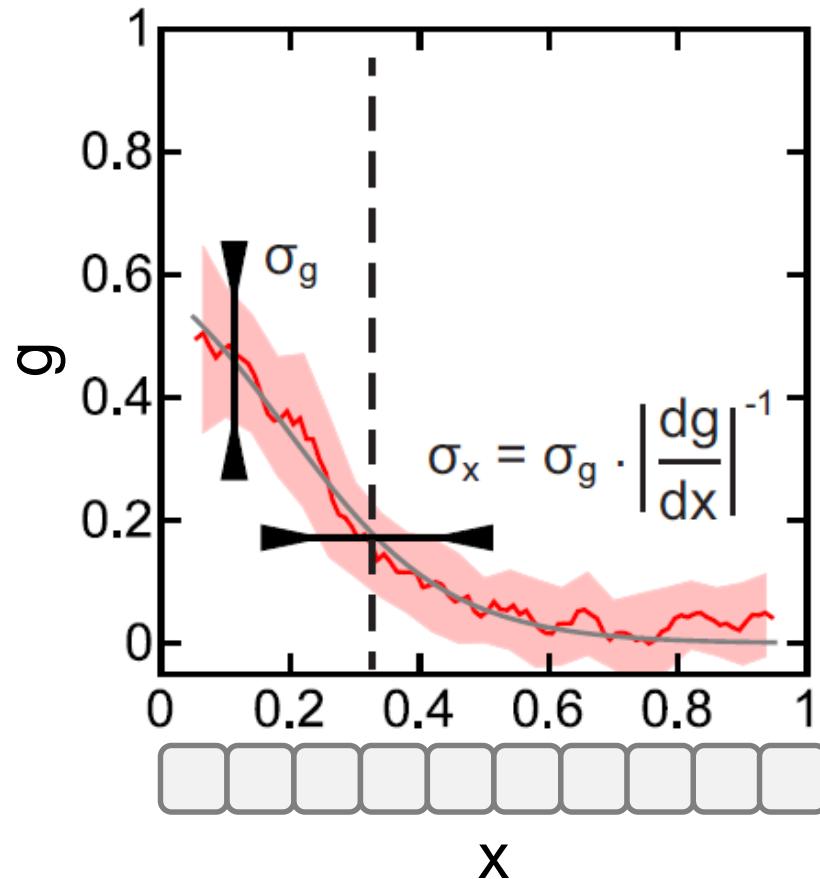


- ▶ Positional information conveyed in the input signals corresponds to positional imprecision in the output
- ▶ Positional error is about 1 cell diameter and equally distributed along the anterior-posterior axis

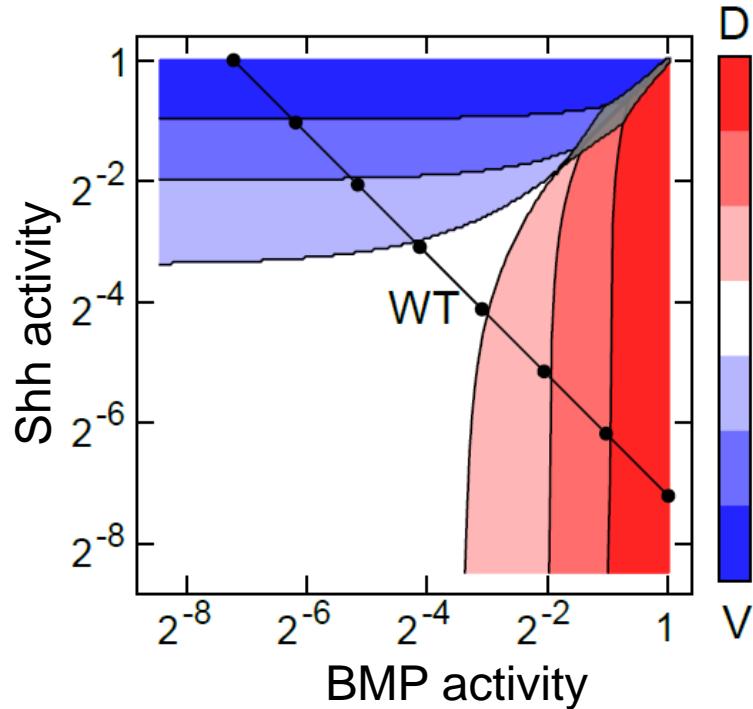


What are the principles of information decoding in development?

Positional error quantifies uncertainty in cell fate specification at a given position



Cells interpret the opposing morphogen signals using an optimal decoding strategy

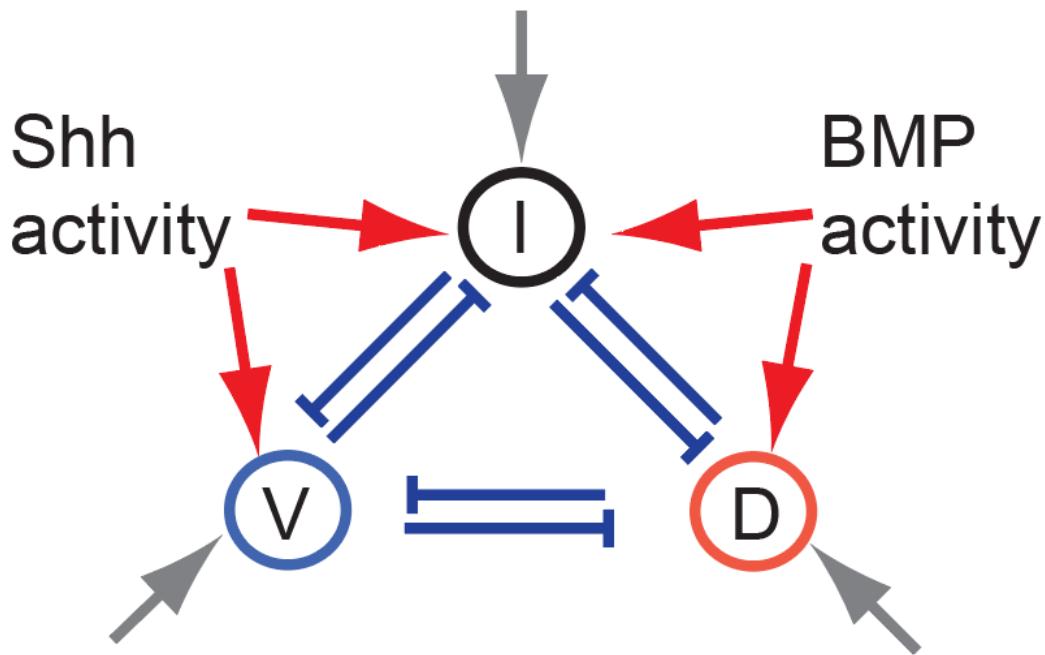


$$P(c_B, c_S|x) = \frac{1}{2\pi\sigma_B(x)\sigma_S(x)} \exp \left\{ -\frac{1}{2} \left[\frac{(c_B - c_B(x))^2}{\sigma_B^2(x)} + \frac{(c_S - c_S(x))^2}{\sigma_S^2(x)} \right] \right\}$$

$$\hat{x}(c_B, c_S) = \operatorname{argmax}_x P(c_B, c_S|x)$$

Morishita & Yoh, PRE, 2009
Tkacik et al., Genetics, 2015
Zagorski et al., Science, 2017

The morphogens activate gene regulatory network (GRN) to specify cell fate



D: Pax3
I: Dbx2
V: Nkx6.1

Numerical screening through GRNs with experimentally motivated criteria

1. Stable gene domains

2. Stripped gene pattern

3. Correct shifts in WT pattern

4. Consistent shifts in Shh mutant

5. High heterogeneity for high signal levels

6. Robustness towards perturbation in init. cond.

Number of GRNs

$\sim 10^8$

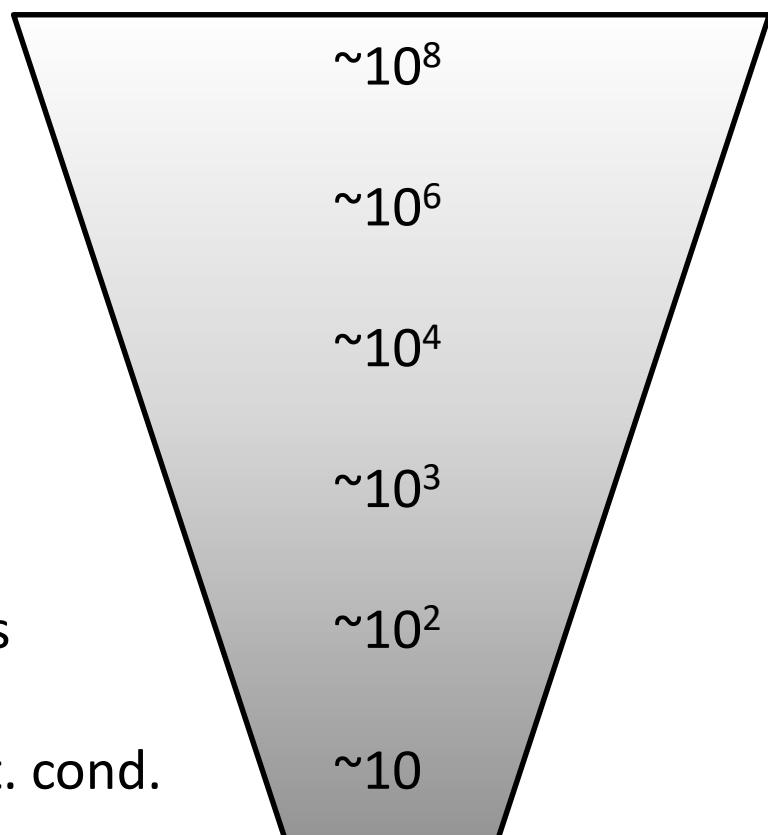
$\sim 10^6$

$\sim 10^4$

$\sim 10^3$

$\sim 10^2$

~ 10



3-node regulatory network model

$$\frac{d[Msx]}{dt} = \alpha_{Msx} \frac{\kappa_{Msx} + c_{B \rightarrow M} \kappa_{Msx} [\text{BMP}]}{(1 + K_{N \rightarrow M} [Nkx])^{m_{N \rightarrow M}} (1 + K_{D \rightarrow M} [Dbx])^{m_{D \rightarrow M}} + \kappa_{Msx} + c_{B \rightarrow M} \kappa_{Msx} [\text{BMP}]} - \gamma_{Msx} [Msx]$$

$$\frac{d[Nkx]}{dt} = \alpha_{Nkx} \frac{\kappa_{Nkx} + c_{S \rightarrow N} \kappa_{Nkx} [\text{Shh}]}{(1 + K_{M \rightarrow N} [Msx])^{m_{M \rightarrow N}} (1 + K_{D \rightarrow N} [Dbx])^{m_{D \rightarrow N}} + \kappa_{Nkx} + c_{S \rightarrow N} \kappa_{Nkx} [\text{Shh}]} - \gamma_{Nkx} [Nkx]$$

$$\frac{d[Dbx]}{dt} = \alpha_{Dbx} \frac{\kappa_{Dbx} + c_{S \rightarrow D} \kappa_{Dbx} [\text{Shh}] + c_{B \rightarrow D} \kappa_{Dbx} [\text{BMP}]}{(1 + K_{M \rightarrow D} [Msx])^{m_{M \rightarrow D}} (1 + K_{N \rightarrow D} [Dbx])^{m_{N \rightarrow D}} + \kappa_{Dbx} + c_{S \rightarrow D} \kappa_{Dbx} [\text{Shh}] + c_{B \rightarrow D} \kappa_{Dbx} [\text{BMP}]} - \gamma_{Dbx} [Dbx]$$

Exhaustive and/or random screen for 3+6+4=13 parameters

$\kappa_{Msx}, \kappa_{Nkx}, \kappa_{Dbx}$

uniform activation, range [0, 5]

$K_{N \rightarrow M}, K_{M \rightarrow N}, K_{N \rightarrow D}, K_{D \rightarrow N}, K_{M \rightarrow D}, K_{D \rightarrow M}$

repressor binding affinity, range [0, 100]

$c_{B \rightarrow M}, c_{B \rightarrow D}, c_{S \rightarrow N}, c_{S \rightarrow D}$

morphogen activation, range [0, 20]

Fixed during screen

$\alpha_{Msx} = \alpha_{Nkx} = \alpha_{Dbx} = 1 (h^{-1})$

production rate

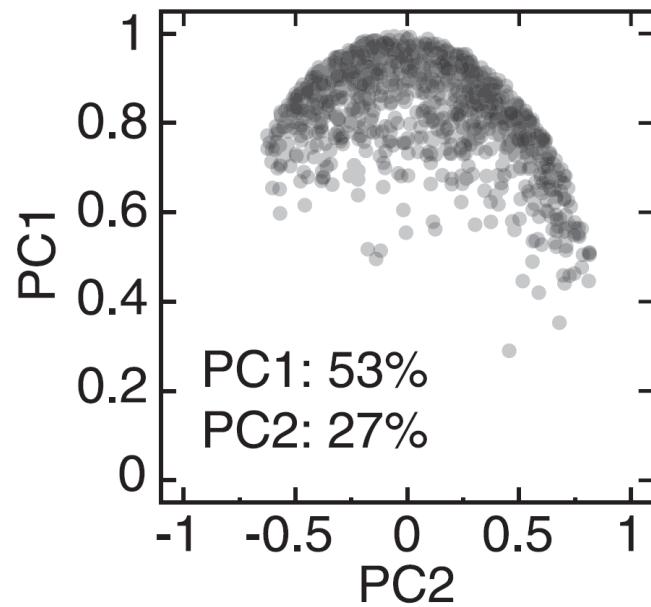
$\gamma_{Msx} = \gamma_{Nkx} = \gamma_{Dbx} = 0.2 (h^{-1})$

degradation rate

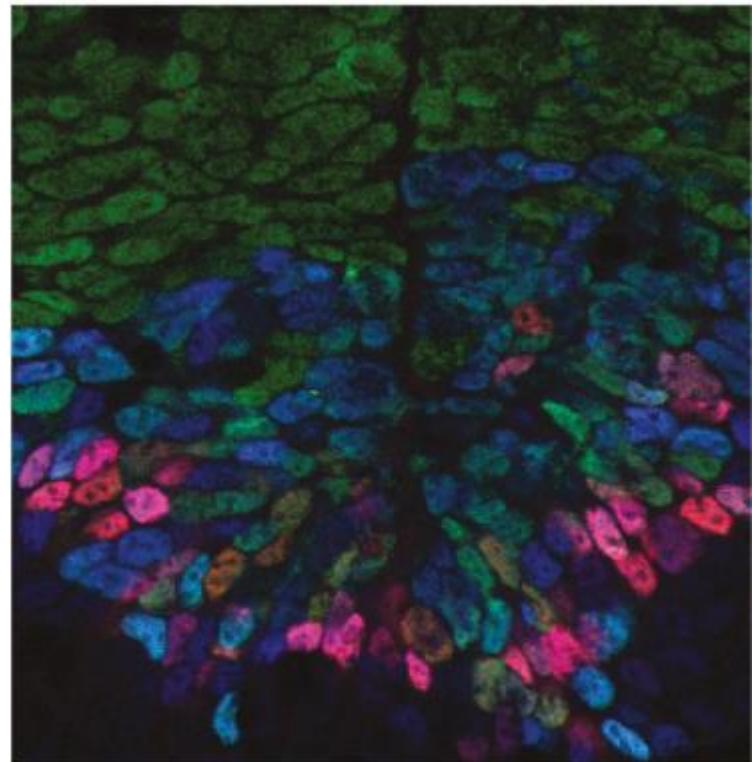
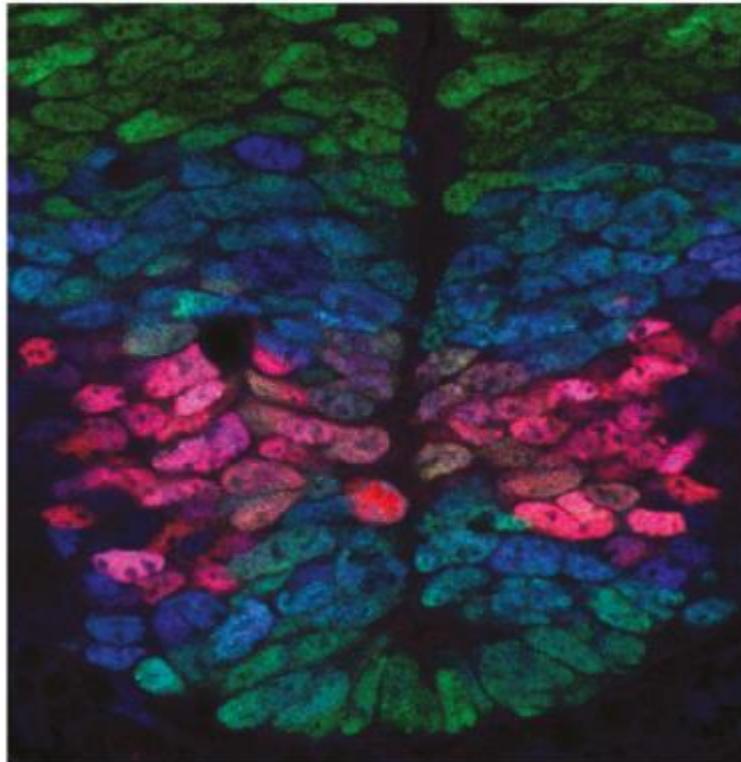
$m_{N \rightarrow M} = m_{M \rightarrow N} = m_{N \rightarrow D} = m_{D \rightarrow N} = m_{M \rightarrow D} = m_{D \rightarrow M} = 2$

Hill coefficients

Successful GRNs formed a single cluster in the parameter space



The pattern is established with less than 3 cell

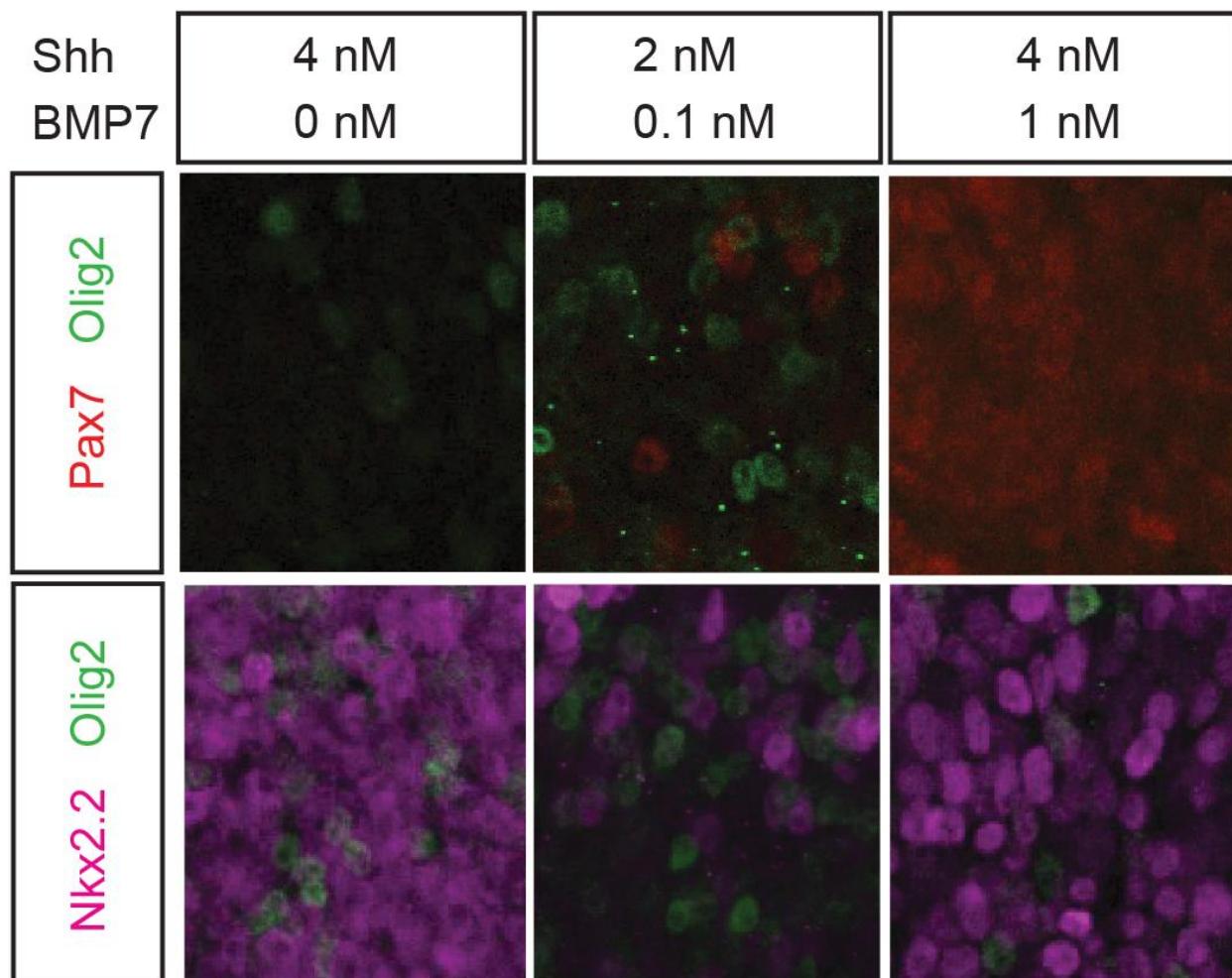
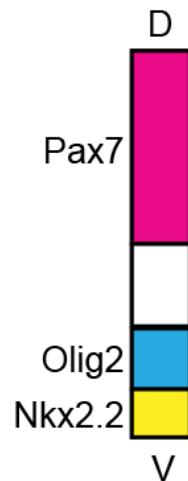
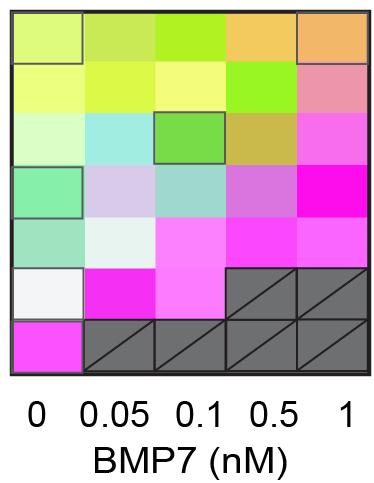


- ▶ Regulatory mechanisms; To what extent the FP size affects the resulting Shh morphogen profile?

Source: [Zagorski et al., Science 356, 2017](#)

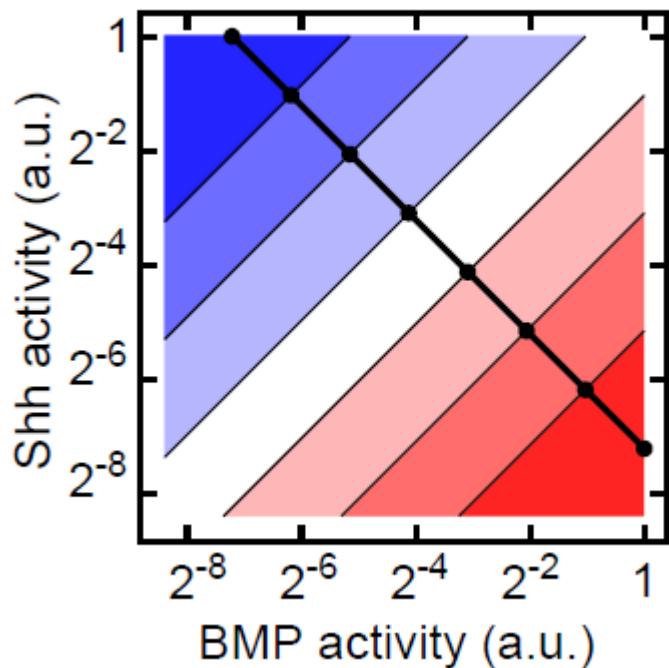
Decoding map reconstructed from explant experiment is consistent with ML predictions

Olig2+Pax7+Nkx2.2

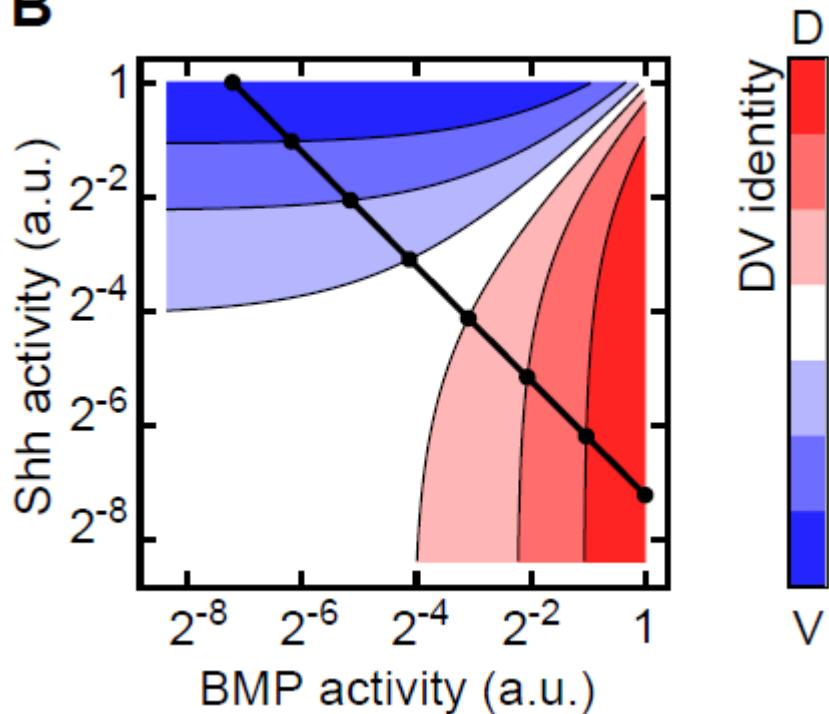


Alternative decoding maps: signal ratio and signal difference

A

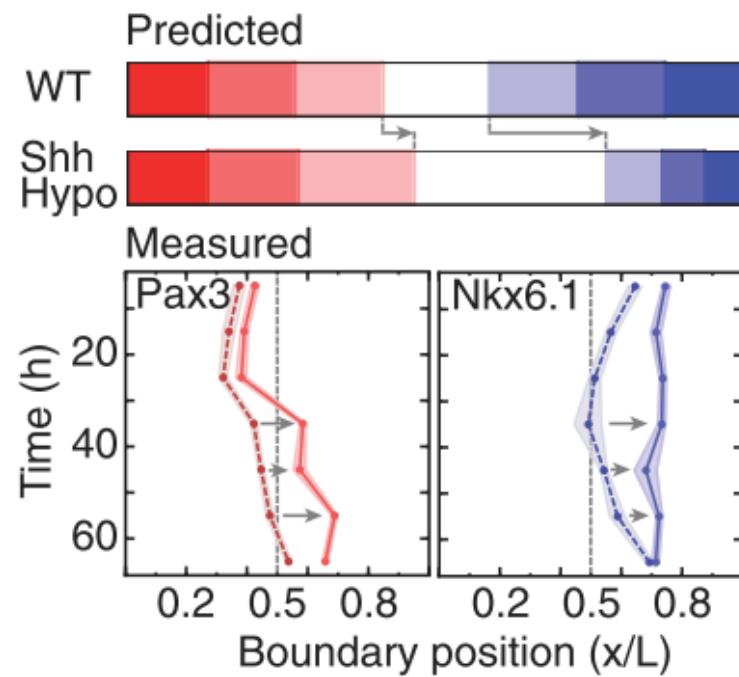
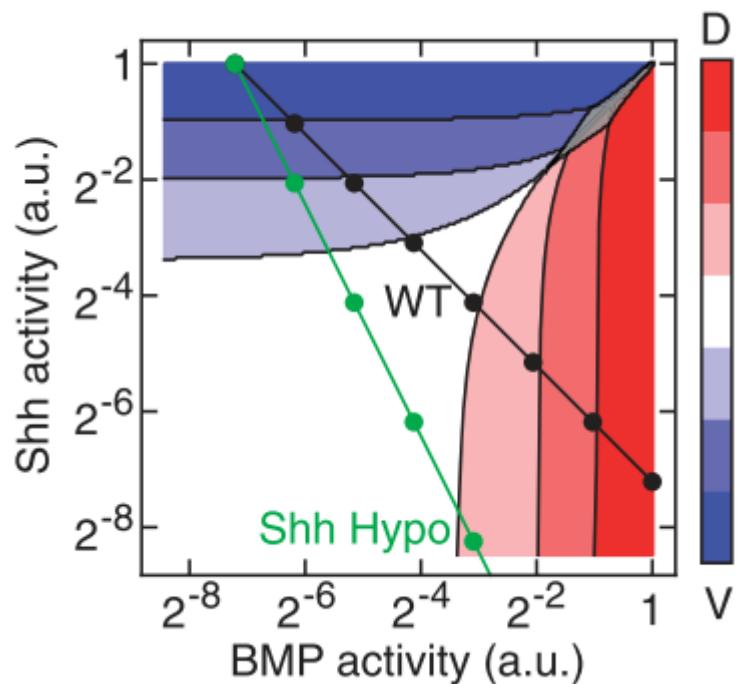


B

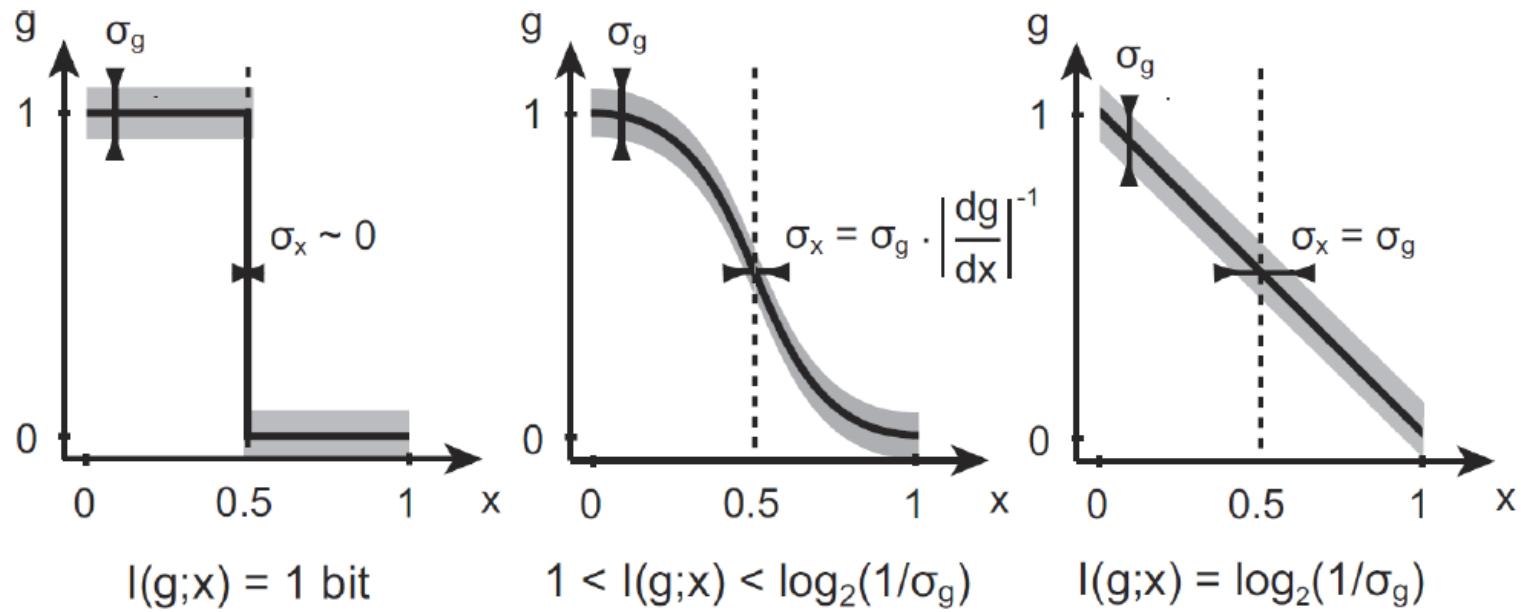


DV identity
D
V

Predictions for Shh deficient mutant (Shh hypomorph)



Positional information in bits



$$I(x \rightarrow \{g_i\}) = \int dx P_x(x) \int d^N \mathbf{g} P(\{g_i\}|x) \log_2 \frac{P(\{g_i\}|x)}{P_g(\{g_i\})}$$

Positional information in bits

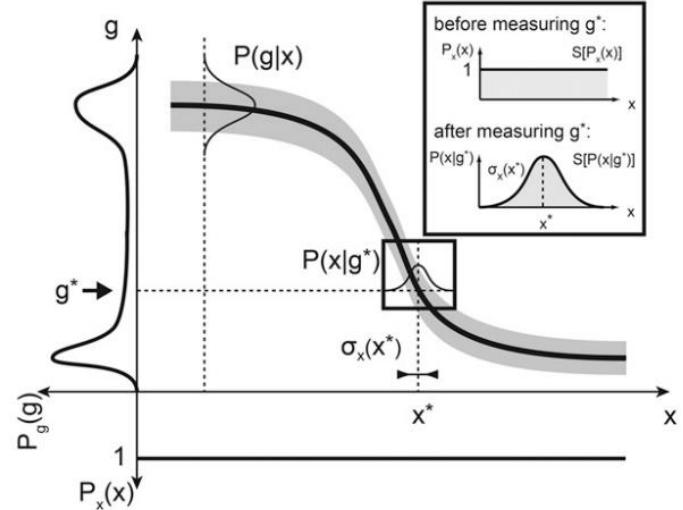
$$S[P_x(x)] = - \int dx P_x(x) \log_2 [P_x(x)]$$

$$I(g) = S[P_x(x)] - S[P(x|g)]$$

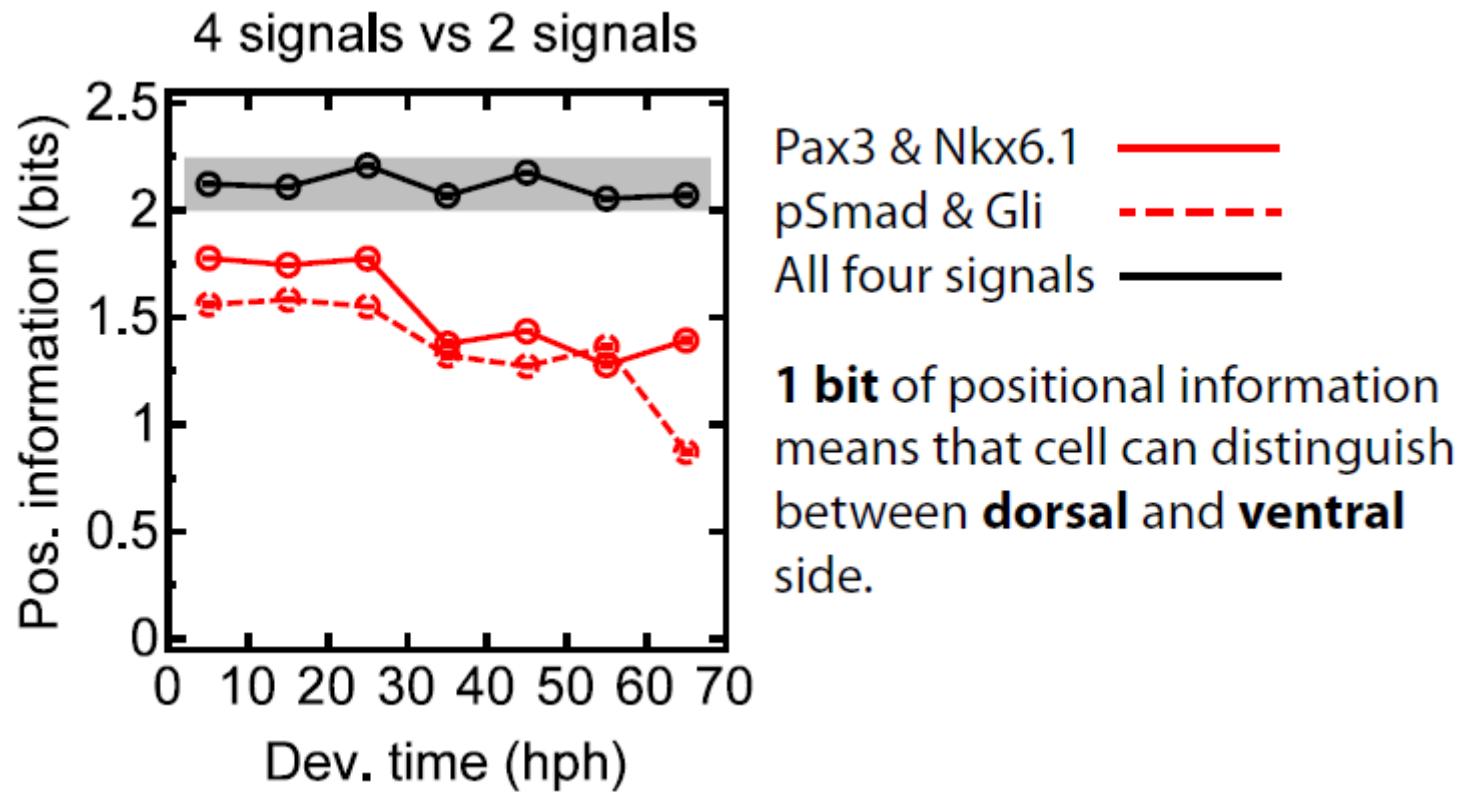
$$I_{g \rightarrow x} = \int dg P_g(g) (S[P_x(x)] - S[P(x|g)]),$$

$$= \int dg \int dx P(g,x) \log_2 \left[\frac{P(g,x)}{P_g(g)P_x(x)} \right]$$

$$I_{g \rightarrow x} = \int dx P_x(x) (S[P_g(g)] - S[P(g|x)])$$

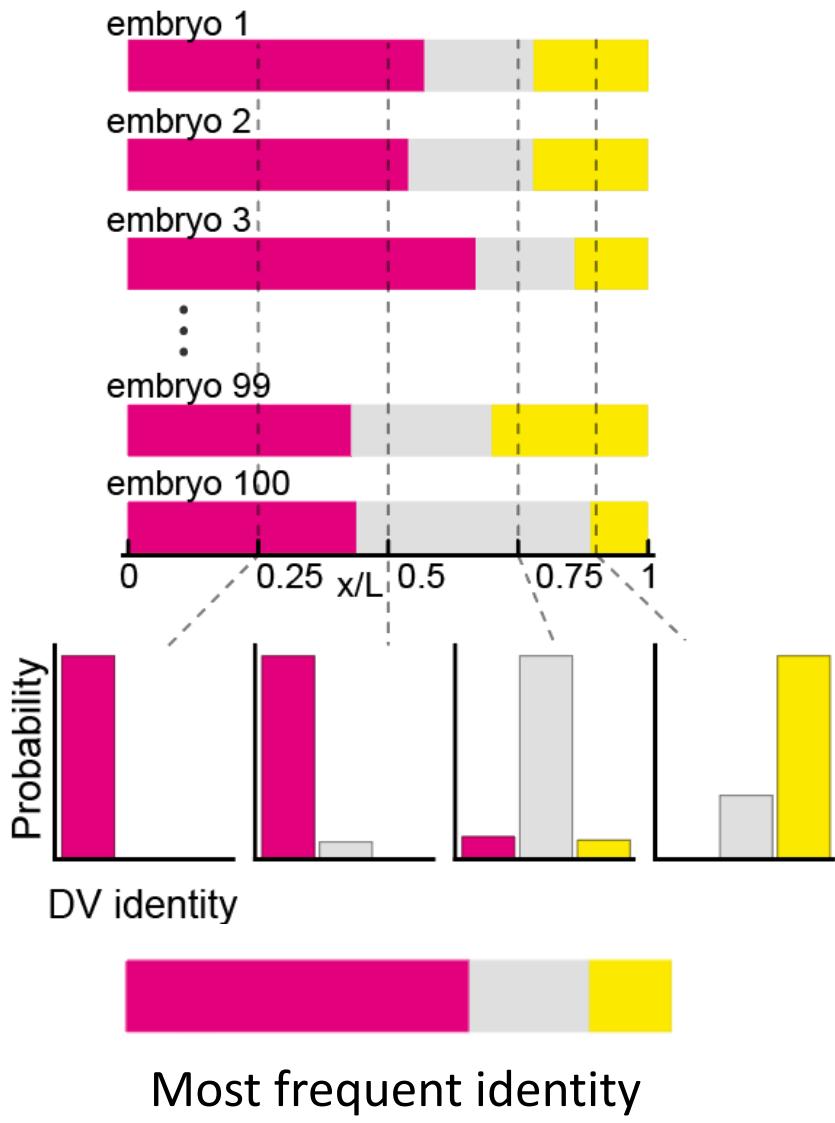
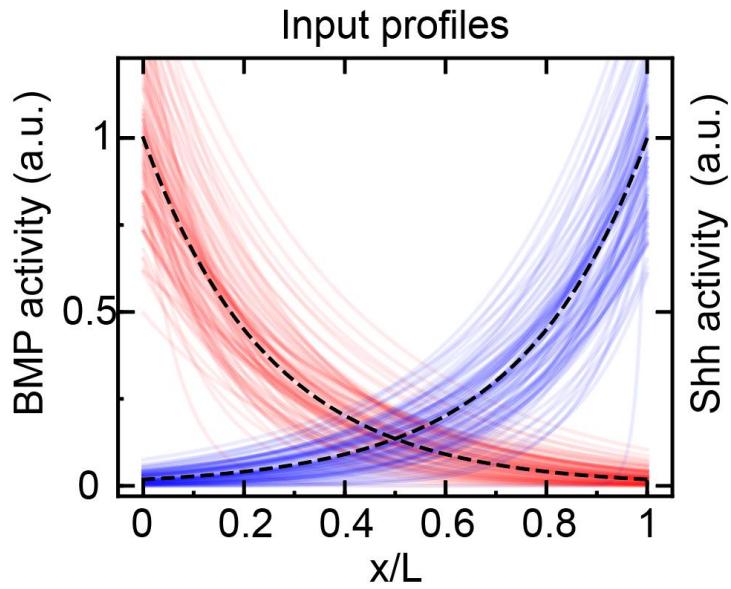
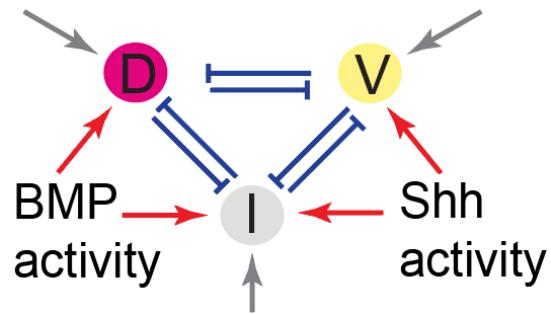


Total positional information is conserved

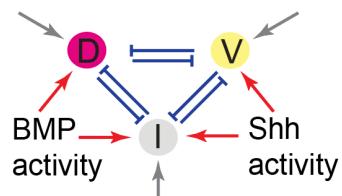


- ▶ Information is transferred from morphogen signals to their target genes at early stages

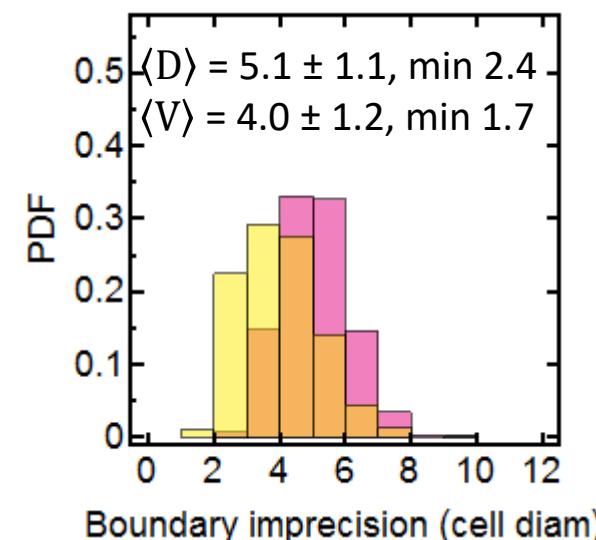
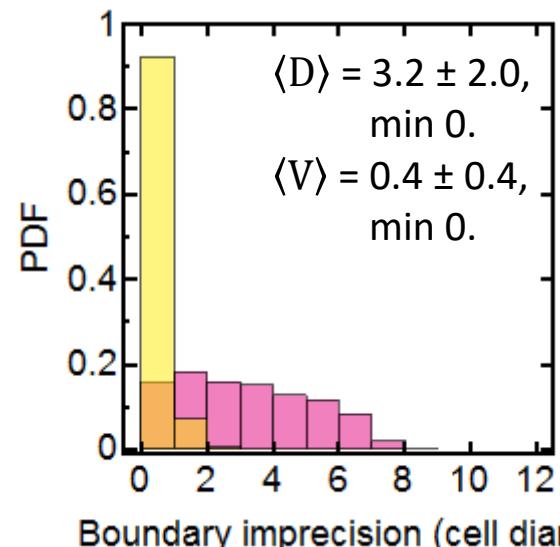
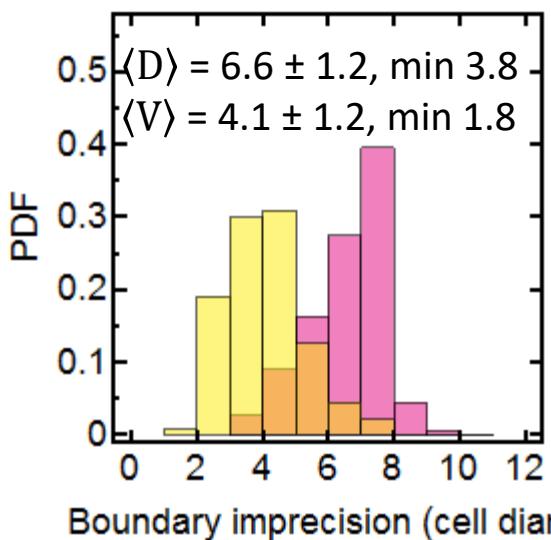
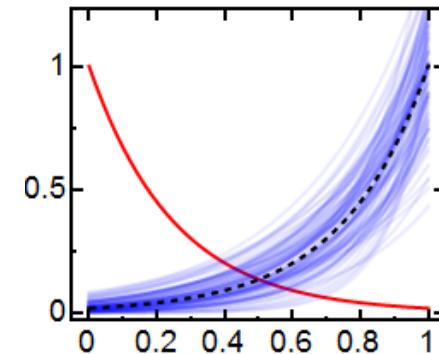
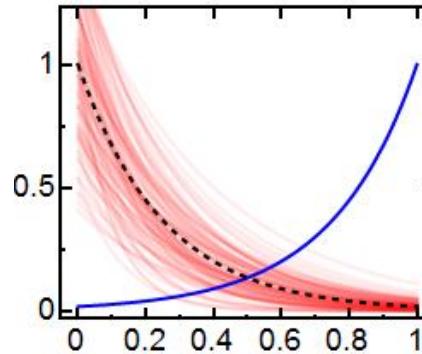
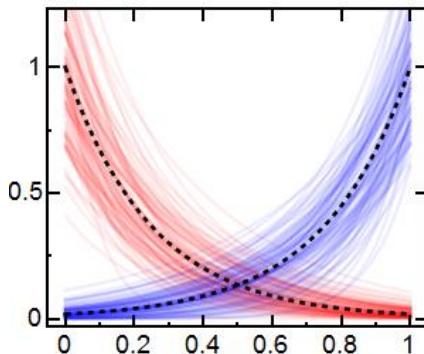
Noise affects resulting striped pattern



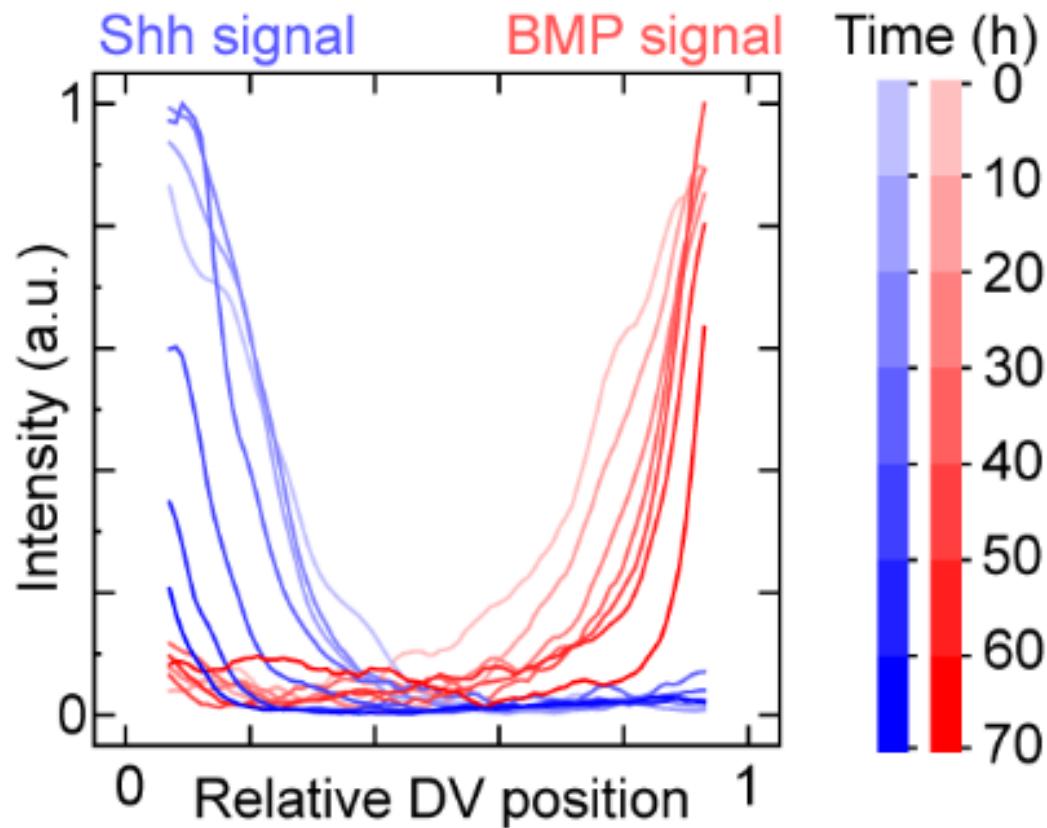
Boundary imprecision for a set of GRNs



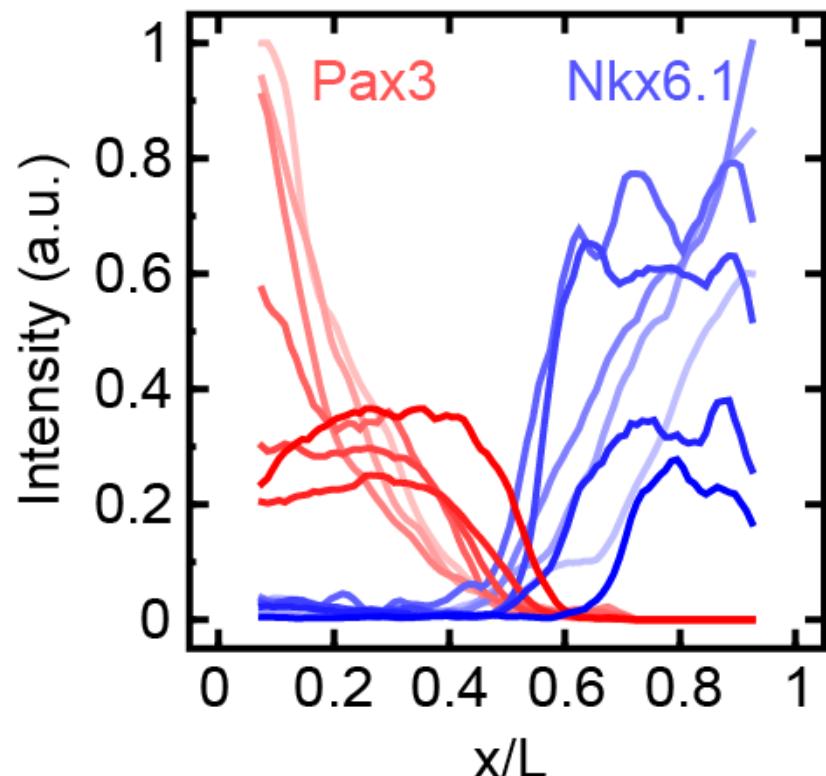
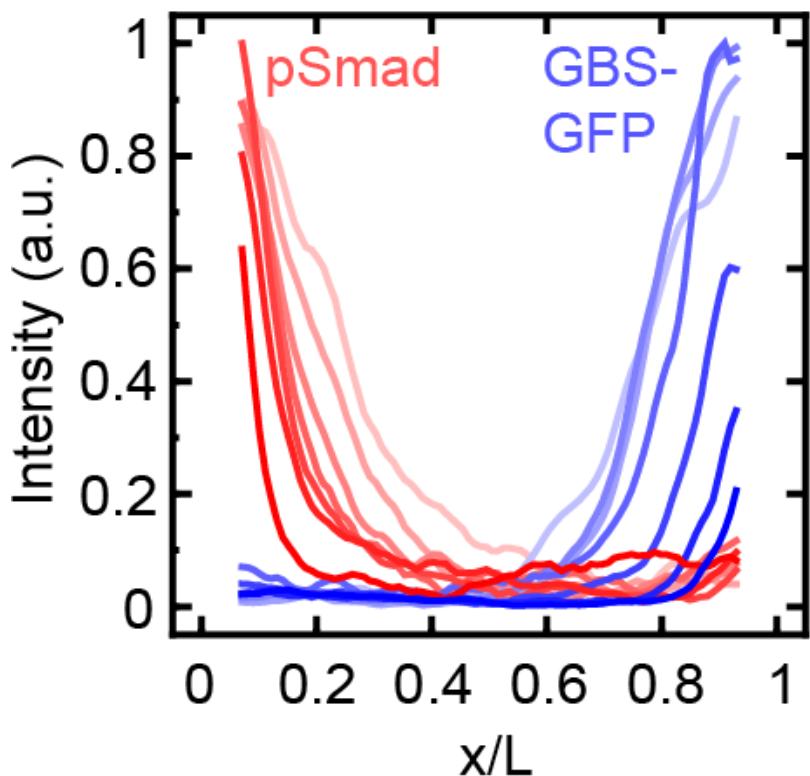
► 1221 GRNs consistent with experimental observations



The morphogen signaling profiles do not scale with the embryo size

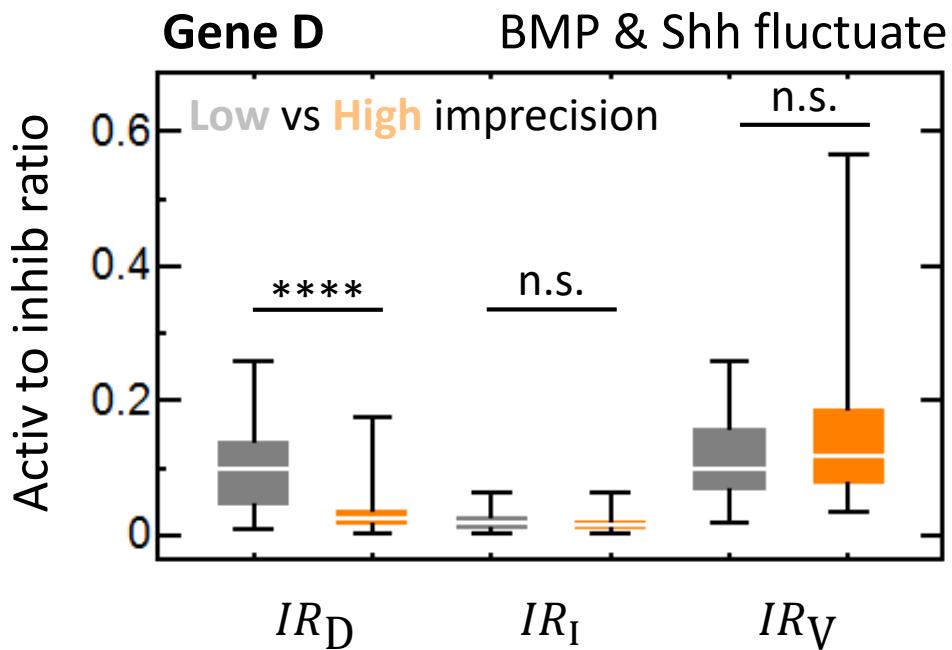


Sharp gene domain boundaries are formed after 30h



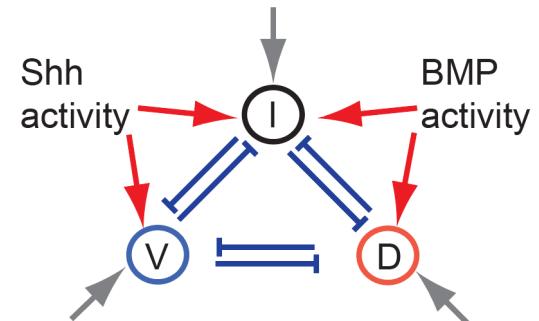
- Are morphogen signals sufficiently precise to specify the positions of target gene expression domains?

Ratio of activatory to inhibitory input of D gene affects boundary imprecision

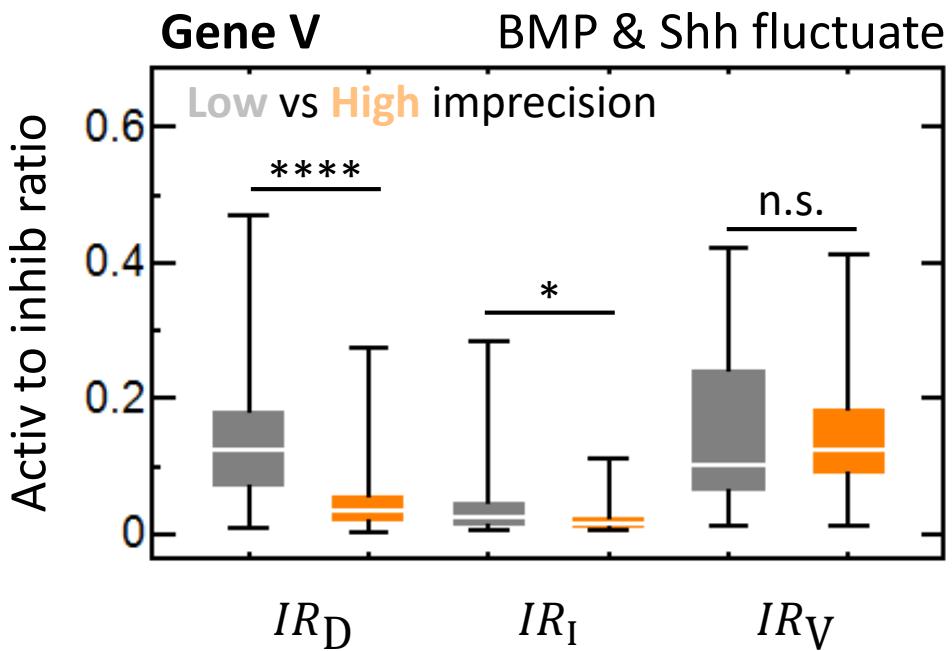


$$IR_{\text{gene}} = \frac{\sum \text{gene}_{\text{activation}}}{\sum \text{gene}_{\text{inhibition}}}$$

$$IR_D = \frac{c_{B \rightarrow D}}{K_{V \rightarrow D} + K_{I \rightarrow D}}$$

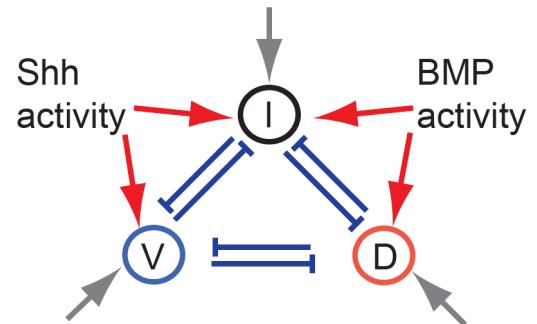


Ratio of activatory to inhibitory input of D gene affects boundary imprecision



$$IR_{\text{gene}} = \frac{\sum \text{gene}_{\text{activation}}}{\sum \text{gene}_{\text{inhibition}}}$$

$$IR_D = \frac{c_{B \rightarrow D}}{K_{V \rightarrow D} + K_{I \rightarrow D}}$$



Ratio of activ to inhib input in GRNs results in different imprecision for only BMP or BMP & Shh fluctuations

