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Kinetic equation for the pair distribution function \\\n in the Boltzmanns gas

We report on a new kinetic equation for an auxiliary two-particle distribution function

$f(\mathbf{k}_1, \mathbf{v}_1, \mathbf{k}_2, \mathbf{v}_2, t)$.

Its general form reads

$$\left(\frac{\partial}{\partial t} + \mathbf{v}_1 \cdot \nabla_{\mathbf{k}_1} + \mathbf{v}_2 \cdot \nabla_{\mathbf{k}_2}\right) f(\mathbf{k}_1, \mathbf{v}_1, \mathbf{k}_2, \mathbf{v}_2, t) = \int d\mathbf{r} \mathcal{G}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{r}, t) f(\mathbf{k}_1, \mathbf{v}_1, \mathbf{k}_2, \mathbf{v}_2, t - \tau)$$

with

$$\mathcal{G}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{r}, \tau) \equiv \int d\mathbf{v}^N d\mathbf{r}^N \mathbf{e}^{-i\mathbf{k}_1 \cdot \mathbf{r}_1} \mathbf{e}^{-i\mathbf{k}_2 \cdot \mathbf{r}_2} \mathcal{P} K_N \mathbf{e}^{-\tau \mathcal{L}} (1 - \mathcal{P}) K_N \mathbf{e}^{i\mathbf{k}_1 \cdot \mathbf{r}_1} \mathbf{e}^{i\mathbf{k}_2 \cdot \mathbf{r}_2} \frac{f^0_N(\mathbf{v}^N, \mathbf{r}^N)}{\varphi_M(\mathbf{v}_1) \varphi_M(\mathbf{v}_2)}$$

which is the scattering operator for our problem.

We have applied to this problem the technique of projection operators.

We find that $\mathcal{G}(t)$ is finite at $t = 0$ and can be readily expanded in Taylor series about $t = 0$. This is a distinct feature which is not present usually in other kinetic equations. Therefore the kinetic equation (1) with the kernel (2) is not only valid for long times but for arbitrarily short times, including $t = 0$, as well.

Next we set the distance between particles 1 and 2, $|\mathbf{r}_1 - \mathbf{r}_2| = a = \text{constant}$. This creates a dumbbell model of molecule, the diffusion of which is being studied.

Summary

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