

Probing the limits of quantum theory in high energy physics.

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of Gdańsk



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OF TECHNOLOGY

Kraków, 11 May 2023

Routes towards New Physics

Standard Model \subset QFT = Quantum Mechanics + Special Relativity

Routes towards New Physics:

- 1 Beyond Standard Model, but still in QFT
 - SUSY, composite Higgs, dark sector, inflation, ...
- 2 Beyond Special Relativity, but assuming QM
 - QFT in curved spacetimes – 'semi-classical' (Unruh effect, ...)
 - quantum gravity
- 3 Beyond Quantum Mechanics, but assuming relativity

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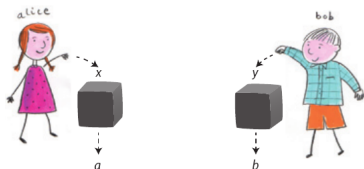
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Bell nonlocality – the **black box** approach

2 parties (Alice and Bob) — 2 **inputs** (x, y) — 2 **outputs** (a, b)

$$P(a, b | x, y)$$



[Sandu Popescu, *Nature Physics* 10, 264 (2014)]

The *experimental* (frequency) correlation function:

$$C_e(x, y) = \frac{N_{++} + N_{--} - N_{+-} - N_{-+}}{N_{++} + N_{--} + N_{+-} + N_{-+}}$$

Local hidden variables [Bell (1964) / Clauser, Horne, Shimony, Holt (1969)]

$$S_{\text{LHV}} := C_{\text{LHV}}(x, y) + C_{\text{LHV}}(x, y') + C_{\text{LHV}}(x', y) - C_{\text{LHV}}(x', y') \leq 2$$

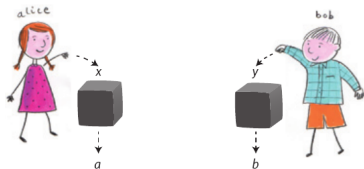
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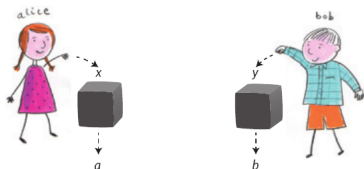
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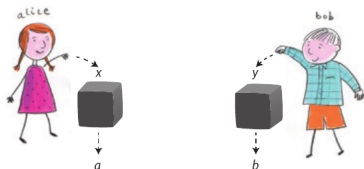
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Bell nonlocality — *beyond* quantum mechanics

$$S := C(x, y) + C(x, y') + C(x', y) - C(x', y')$$

Can we achieve $S = 4$?

- Alice and Bob can communicate,
- or their settings are pre-correlated.

But can we do it assuming:

- **no-signalling**: $\sum_b P(a, b | x, y) = \sum_b P(a, b | x, y')$, for all a, x, y, y' ,
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- **freedom of choice**: $P(x, y | \lambda) = P(x) \cdot P(y)$?

No-signalling boxes [Popescu, Rohrlich (1994)]

$$P(a, b | x, y) = \begin{cases} \frac{1}{2}, & \text{if } a \oplus b = xy, \\ 0, & \text{otherwise,} \end{cases} \quad S_{\text{PR}} = 4.$$

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1 Beyond-quantum correlations

- No-signalling boxes

[N. Brunner, D. Cavalcanti, S. Pironio, V. Scarani, S. Wehner, *Rev. Mod. Phys.* **86**, 419 (2014)]

- 3-party monogamy violation

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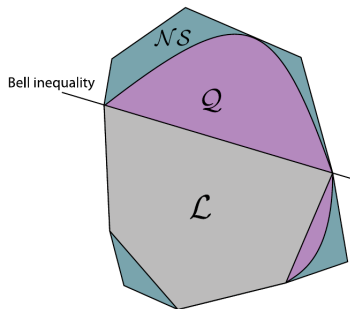
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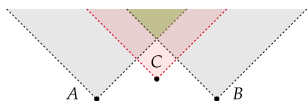
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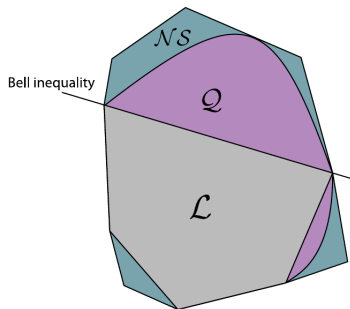
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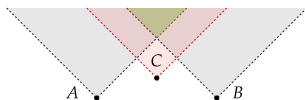
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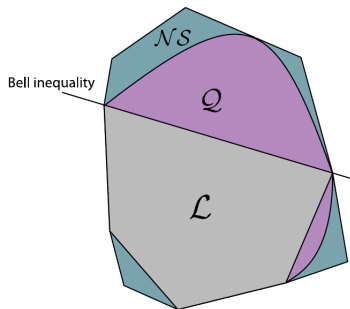
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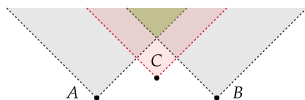
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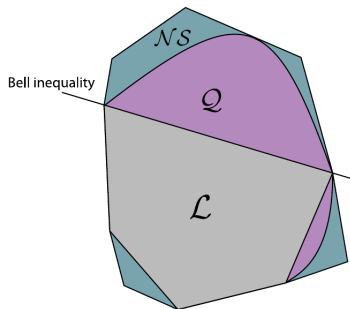
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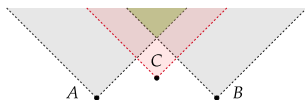
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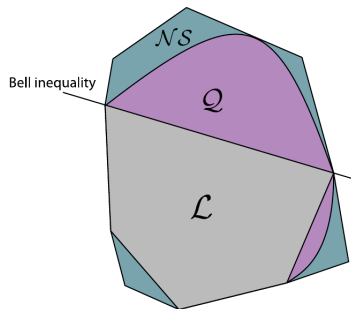
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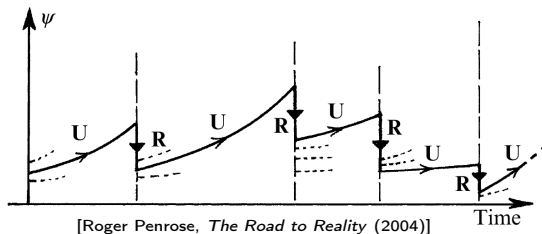


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Purely operational 'theories' — model-independent approach

Objective collapse models

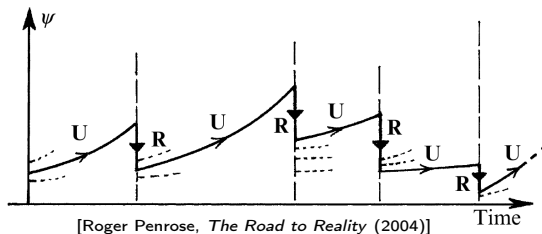


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- **nonlinearity** — modified Schrödinger equation
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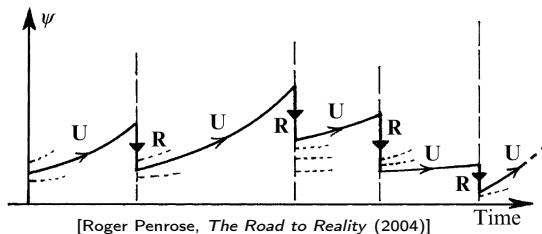


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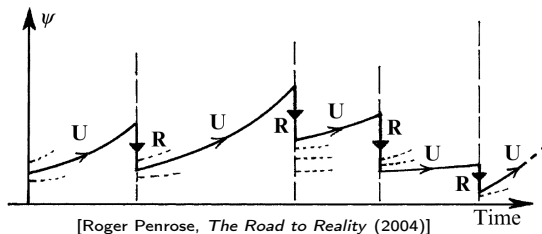


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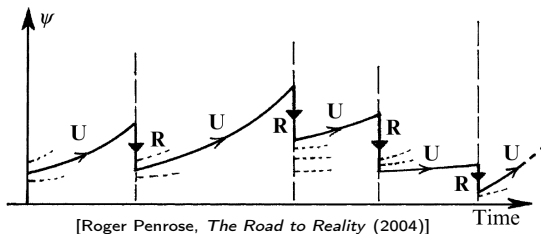


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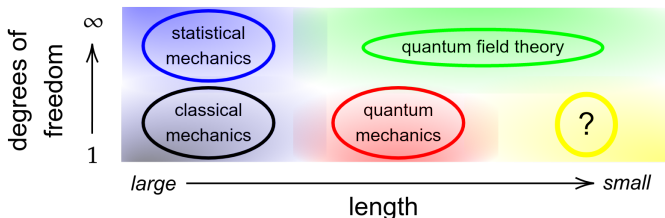
3 Wave function collapse models

[A. Bassi, K. Lochan, S. Satin, T.P. Singh, H. Ulbricht, *Rev. Mod. Phys.* **85**, 471 (2013)]

- Aimed at explaining the 'quantum-to-classical' transition.
- **nonlinearity** — modified Schrödinger equation
- **stochasticity** — 'collapse noise'

Objective collapse models involve deviations from unitarity and linearity.

Beyond-quantum physics?



- Is there a gap between QM and QFT?

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$$|\psi\rangle \in \mathcal{H}_A \otimes \mathcal{H}_B,$$

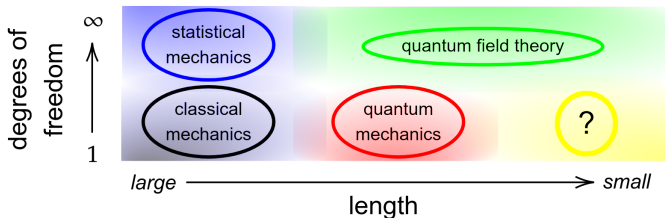
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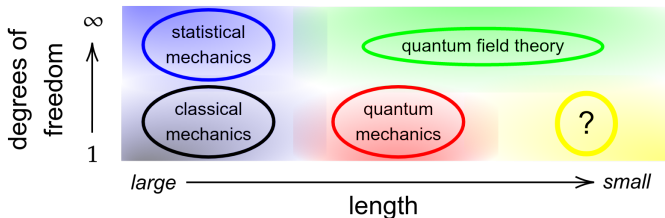
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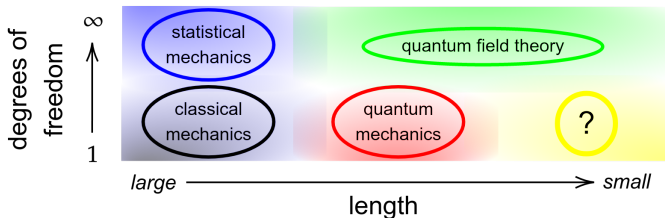
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Quantum-data boxes

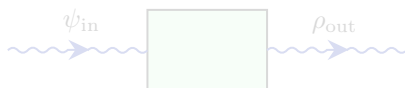
- We regard physical systems (e.g. a single nucleon) as **Q-data boxes**, i.e. quantum-information processing devices.
- A Q-data box is probed *locally* with quantum information.



- p are classical parameters (e.g. scattering kinematics)
- The *pure input* state is **prepared**, $P : x \rightarrow \psi_{\text{in}}$.
- The *output state* is reconstructed via **quantum tomography** from the outcomes of projective measurements $M : \rho_{\text{out}} \rightarrow a$.

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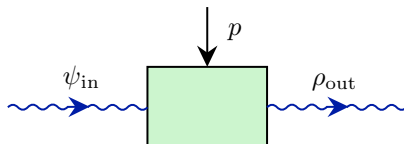
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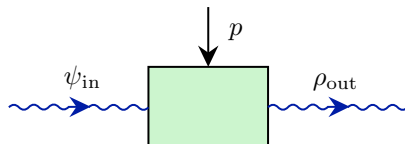
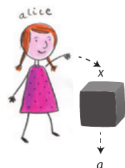
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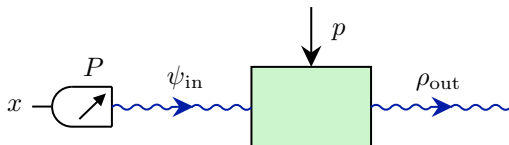
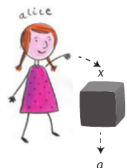


[Nat. Phys. 10, 264 (2014)]

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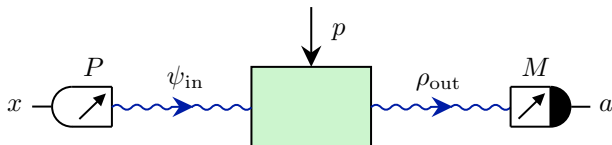
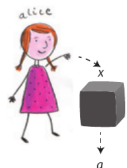


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Quantum preparation and tomography

Quantum state preparation:

- In principle, any quantum state can be prepared via proj. measurements.
- ψ_{in} is pure, uncorrelated with the box — 'freedom of choice'.

Quantum state tomography:

- A mixed state ρ_{out} on \mathcal{H} is an $n \times n$ matrix, with $n = \dim \mathcal{H}$.
- Take a complete set of projectors $\{M_i\}_{i=1}^{n^2-1}$ (e.g. $\{\sigma_x, \sigma_y, \sigma_z\}$).
- Make *multiple* measurements and register $\{P(a_j | M_i)\}_{i,j}$
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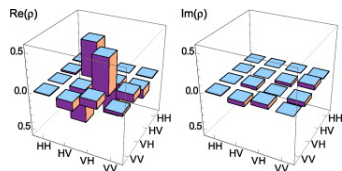
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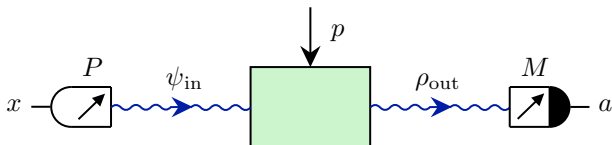
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[J. Huwer et al., *New J. Phys.* 15, 025033 (2013)]

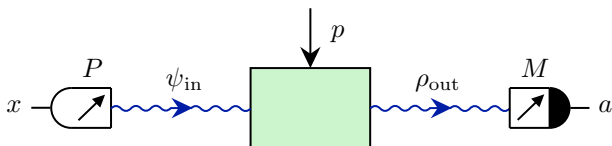
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A **Q-data test** consists in probing a given Q-data box with *prepared* input states.

- For every input state ψ_{in} one needs to perform the full tomography of ρ_{out} .
- A Q-data test yields a dataset $\{\psi_{\text{in}}^{(k)}, p^{(\ell)}; \rho_{\text{out}}^{(k,\ell)}\}_{k,\ell}$.
- The more tomographic measurements, the more reliable the test.
- The input ψ_{in} is pure, but the output ρ_{out} is *mixed*.

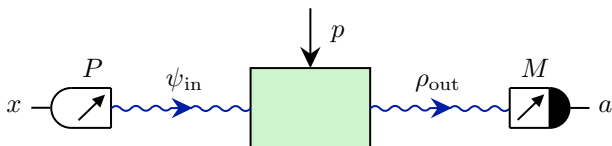
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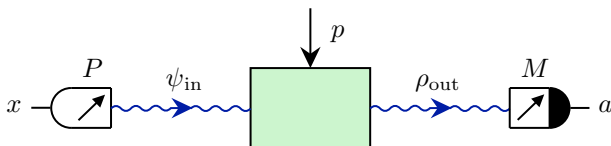
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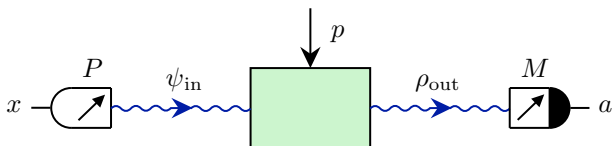
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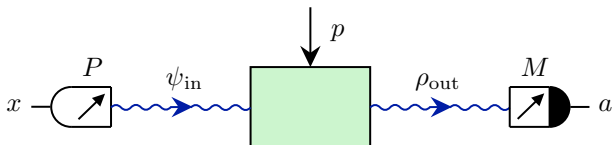
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An example — the Helstrom test

- Suppose that we have two available inputs $\psi_{\text{in}}^{(1)}, \psi_{\text{in}}^{(2)}$.
- We choose randomly the input (with probability $1/2$).
- The task is to guess, which of the two states was input.
- Define the **success rate**: $P_{\text{succ}}(\psi_{\text{in}}^{(1)}, \psi_{\text{in}}^{(2)}) := \frac{1}{2} \sum_{k=1}^2 P(a = k | \psi_{\text{in}}^{(k)})$.
- In quantum theory P_{succ} cannot exceed the **Helstrom bound**

$$P_{\text{succ}} \leq P_{\text{succ}}^{\text{QM}} := \frac{1}{2} \left(1 + \sqrt{1 - |\langle \psi_{\text{in}}^{(1)} | \psi_{\text{in}}^{(2)} \rangle|^2} \right).$$

- Make a Q-data test with $\{\psi_{\text{in}}^{(k)}; \rho_{\text{out}}^{(k)}\}_{k=1,2}$.
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- QM implies that any **quantum channel**, i.e. a map $\mathcal{E} : S(\mathcal{H}_{\text{in}}) \rightarrow S(\mathcal{H}_{\text{out}})$ is completely positive trace preserving (**CPTP**).

Kraus' theorem

For every CPTP map $\mathcal{E} : S(\mathcal{H}_{\text{in}}) \rightarrow S(\mathcal{H}_{\text{out}})$ there exists a (non-unique) set of operators $\{K_i\}_{i \leq mn}$, where $m = \dim \mathcal{H}_{\text{in}}$, $n = \dim \mathcal{H}_{\text{out}}$, such that

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\mathcal{E} is CPTP if and only if $\tilde{\mathcal{E}} = \frac{1}{m} \sum_{i,j=1}^m |i\rangle\langle j| \otimes \mathcal{E}(|i\rangle\langle j|) \in \mathbb{C}^{mn \times mn}$ is a state.

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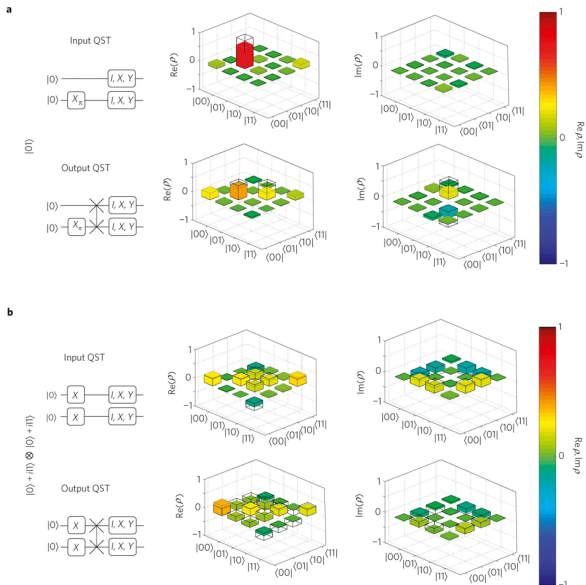
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[R. Bialczak et al., *Nature Physics* **6**, 409 (2010)]



Towards experimental quantum process tomography

- 1 Prepare a 'quantum-programmed' particle carrying ψ_{in} , e.g. electron's spin or photon's polarization.
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- Need to prepare the quantum state of GeV particles \rightsquigarrow polarized beams
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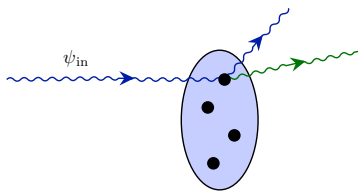


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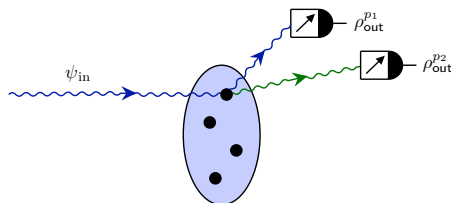
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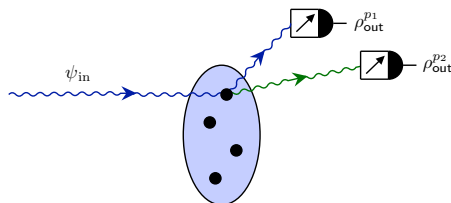


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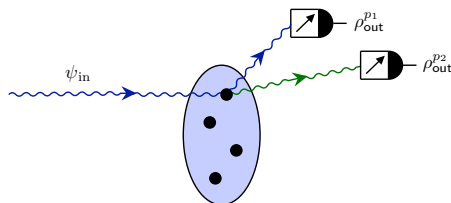


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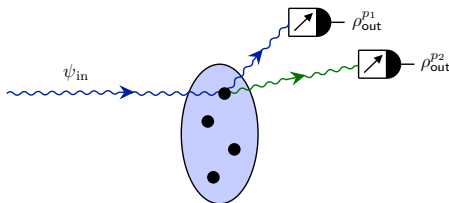


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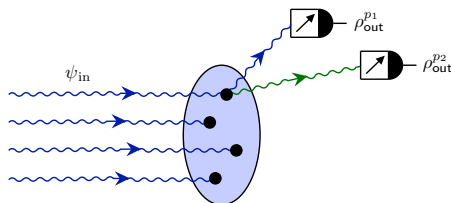
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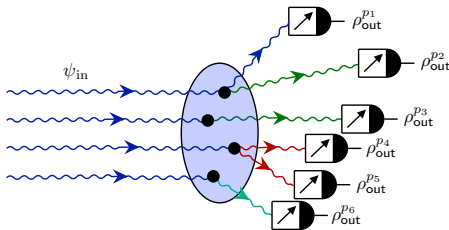
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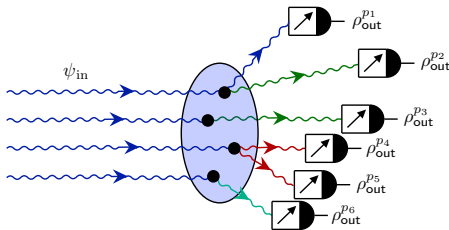
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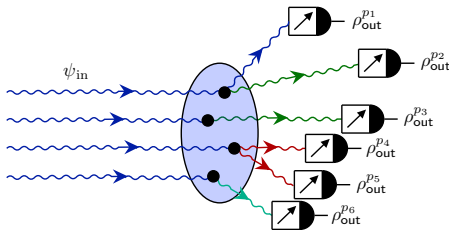
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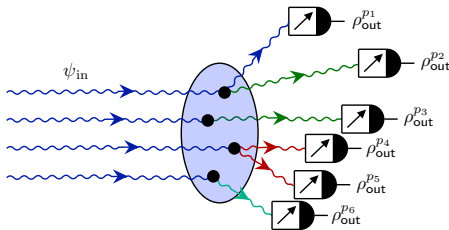
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Proc. R. Soc. A. **478**:20210806 (2022), arXiv:2103.12000

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- Whenever we are doing a Bell-type test, we are testing QM against *both* local hidden variables and **beyond-quantum correlations**.
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